

VALUING EQUITY IN DISTRESSED FIRMS

Problem 1

- a. True. Equity investors cannot lose more than their equity investment.
- b. False. They can make equity more valuable, not the firm.
- c. True. It transfers wealth to the bondholders.
- d. True. This is the equivalent of the life of the option.
- e. True. There is a transfer of wealth to bondholders.

Problem 2

- a. Reinvestment rate = $g/ROC = 5\%/12\% = 41.67\%$
 Value of the firm = $40(1.05)(1-.5)(1-0.4)/(.10-.05) = \294 million

b.

The value of the equity is computed as a call option on the value of the firm, using the call

option pricing formula, $SN(d_1) - Ke^{-rt}N(d_2)$, where $d_1 = \frac{\ln(S/K) + (r + \sigma^2/2)t}{\sigma\sqrt{t}}$, $d_2 =$

$d_1 - \sigma\sqrt{t}$.

S = \$294

K = \$500

t = 5 years

r = 5%

$\sigma = 0.125$

The equity or call option value can be written as $294 N(-0.8657) - 500 e^{-0.25} N(-1.1452)$.

Since $N(d_1) = 0.1933$; $N(d_2) = 0.1261$, the option value is \$7.75 million.

Value of Call (Equity) = \$7.75 million

- c. Value of Debt = $\$294 - \$7.75 = \$286.25$ million

Appropriate Interest Rate = $(500/286.25)^{1/5} - 1 = 11.80\%$

Problem 3

Value of firm

Current free cashflow to firm = $\$ 850 * (1-.4) - (550 - 400) = \$ 700$ million

Year	EBIT (1-t)	Net cap ex	FCFF	PV
------	------------	------------	------	----

1	\$612.00	\$180.00	\$432.00	\$392.73
2	\$734.40	\$216.00	\$518.40	\$428.43
3	\$881.28	\$259.20	\$622.08	\$467.38
4	\$1,057.54	\$311.04	\$746.50	\$509.87
5	\$1,269.04	\$373.25	\$895.80	\$556.22
Terminal	\$1,332.50	\$444.17	\$888.33	

I used a reinvestment rate of 33.33% (5/15) in the terminal year.

Terminal value = $888.33 / (.10 - .05) = \$ 17,766$

Value of firm = $392.73 + 428.43 + 467.38 + 509.87 + 556.22 + 17766.60 / 1.1^5 =$
 $\$13,386.28$ million

Value of equity as an option

$S = 13386.28$

$K = 10000.00$

$T =$ Weighted duration of debt = 3 years

Riskless rate = 5%

Variance in firm value = $(.35)(.4)^2 + (.15)(.6)^2 + 2 (.35)(.15)(.5)(.4)(.6) = .20 = 0.0403$

Value of equity = $\$ 4958$ million

If the market value of equity = $30 * 210 = \$ 6300$ million

Trial and error yields an implied standard deviation of 46.53%.

Value of debt = Firm value – Value of equity

= $13386 - 4958 = \$8,428$ million

Problem 4

Value of firm = $EBIT (1-t) (1 - \text{Reinvestment rate}) (1+g)/(r - g)$
 $= 25 (1-.4) (1 - 4/10) (1.04)/(.09-.04) = \$ 187.20$ million

Face value of debt = $\$ 250 + \$ 250 = \$ 500$ million

Average duration of debt = $(2+4)/2 = 3$ years

Standard deviation in firm value = $0.25^2(.5)^2 + 0.4^2(.5)^2 + 2 * .25 * .4 * .5 * (.5)^2 = 28.39\%$

Riskless rate = 7%

Value of equity as an option = $\$ 3.30$ million

Problem 5

$d1 = -0.15$

$N(d1) = 0.4404$

$d2 = -0.90$

$N(d2) = 0.1841$

$$\text{Value of Equity} = 400 (.4404) - 800 \exp(-.06 \cdot 6) (.1841) = \$ 73.41$$

$$\text{Value of Debt} = 400 - 73.41 = \$ 326.59$$

$$\text{Interest rate on debt} = (800/326.59)^{(1/6)} - 1 = 16.08\%$$

$$\text{Default spread on debt} = 16.08\% - 6\% = 10.08\%$$