# EXPECTED RETURN, REALIZED RETURN AND ASSET PRICING TESTS

by

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One of the fundamental issues in finance is what are the factors that affect expected return on assets, the sensitivity of expected return to these factors, and the reward for bearing this sensitivity. There is a long history of testing in this area, and it is clearly one of the most investigated areas in finance.

Almost all of the testing I am aware of involves using realized returns as a proxy for expected returns. The use of average realized returns as a proxy for expected returns relies on a belief that information surprises tend to cancel out over the period of the study and realized returns are therefore an unbiased estimate of expected returns. However, I believe that there is ample evidence that this belief is misplaced. There are periods longer than ten years where stock market realized returns are on average less than the risk-free rate (1973 to 1984). There are periods longer than fifty years in which risky long-term bonds on average underperformed the risk free rate (1927 to 1981). Having a risky asset with an expected return above the riskless rate is an extremely weak condition for realized returns to be an appropriate proxy for expected returns, and eleven and fifty years is an awfully long time for such a weak condition not to be satisfied. In the recent past, the U.S. has had stock market returns over 30 percent per year while Asian markets have had negative returns. Does anyone honestly believe that this is because this was the riskiest period in history for the U.S. and the safest for Asia? In addition, there is a large body of evidence we find anomalous. This includes the effect of inflation on asset pricing and the failure of the generalized expectation theory to explain term premiums. Changing risk premiums and

See Ibbotson (1995) and compare long-term government bond returns to T-bills returns.

conditional asset pricing theories may be a way of "explaining" some of the anomalous results. However, this does not explain returns on risky assets less than the riskless rate for the long periods when it has occurred. It seems to me that the more logical explanation for these anomalous results is that realized returns are a very poor measure of expected returns and that the information surprises highly influence a number of factors in our asset pricing model. I believe that developing better measures of expected return and alternative ways of testing asset pricing theories that do not require using realized returns have a much higher payoff than any additional development of statistical tests that continue to rely on realized returns as a proxy for expected returns. I would like to illustrate what I have in mind by examining the expected return on Government bonds, and then present some preliminary thoughts in the common stock area.

Government bonds are assets where I believe we can obtain much better estimates of expected return from realized return. Government bonds have little asset-specific information that should affect their price.<sup>2</sup> Rather, the factors that affect the prices of Government bonds are in the form of aggregate economic information. There is wide consensus on which economic variables could affect the prices of Government bonds. Variables that are considered potentially important are common across the major players.<sup>3</sup> Furthermore, the time when information about these variables is announced is known and fixed. Finally, the impact of the surprise component in announcements

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The exceptions are liquidity effects and tax effects which are asset-specific. However, these are very small in magnitude and relatively constant over time (see Elton and Green (1998)).

However, which of these variables actually affect prices is a serious research topic. See Balduzzi, Elton and Green (1997) for a careful analysis of this topic.

is rapidly incorporated into prices (see Balduzzi, Elton and Green (1997)). The combination of a common information set, known announcement time, and rapid reflection of information into price allows us to put together a data set unaffected by information surprises and provides a unique opportunity to put together a set of reasonably accurate estimates of expected returns. This data set can then be used to examine some of the hypotheses of what affects expected return on Government bonds. In the first part, I explore some of these ideas. In the second part, I make more speculative comments in the common stock area. Before doing either, however, I would like to expand on my prior thoughts briefly.

#### I. An Overview

Before examining some applications of the ideas it is useful to explore the basic idea some more.

We can think of returns as being decomposed into expected returns and unexpected returns.

More formally:

$$R_{t} = E_{t-1}(R_{t}) + e_{t}$$
 (1)

where  $R_t$  is return in period t,  $E_{t-1}(R_t)$  is expected return at t conditional on information available at t-1,  $e_t$  is unexpected return

In the common stock area unexpected return is viewed as coming from systematic factors or unique firm specific events. In the government bond area unexpected returns result from surprises in the macro economic announcements. The hope in using realized return as a proxy for expected return is that the unexpected returns are independent so that as the observation interval

increases, they tend to a mean of zero. What I'm arguing is that either there are information surprises that are so large or that a sequence of these surprises are correlated so that the cumulative effect is so large that they have a significant permanent effect on the realized mean. Furthermore, these surprises can dominate the estimate of mean returns and be sufficiently large so that they are still a dominant influence as the observation interval increases. Thus, the model I have in mind is

$$R_{t} = E(R_{t-1}) + I_{t} + \boldsymbol{e}_{t} \tag{2}$$

where  $I_t$  is a significant information event.

I view I<sub>t</sub> as mostly zero and occasionally a very large number. Thus I view the e<sub>t</sub> as a mixture of two distributions, one with standard properties and the other that more closely resembles a jump process. Let me discuss some examples. When I first entered the profession, those of us that looked at the efficient frontiers talked about the McDonald Effect. Any data set that included McDonalds showed extremely large returns for very little risk. The use of McDonalds, as an input to an efficient frontier, produced portfolios that consisted almost exclusively of McDonalds and were simply not credible. What was going on? For the first few years, no one anticipated the size of the earnings that McDonald announced and every time earnings were announced the stock soared dramatically. In the formality above, I<sub>t</sub> was very large at earnings announcements and highly correlated. Estimates of the sensitivity were very low given the large shocks. Adding additional observations would dampen the impact, but never eliminate it as the dominant feature of the data. As I discuss later including McDonalds in asset pricing tests causes similar difficulties to using it as an input to the efficient frontier. Earnings surprises for companies in their early

years is an obvious example of what I have in mind. There are a lot of other examples with more mature companies. Atlantic Richfield with North Shore Oil, Pfizer with the announcement of Viagra caused a large one time return that would cause problems for asset pricing tests. Corporate restructuring, such as being acquired, should have a similar effect.

There are similar problems with market returns or factor returns. In the introduction, I mention that long term government bonds earned less than T-bills for over a fifty year period. There is a subsequent five year period where the returns total 112 percent and included yearly returns of 40 percent, 31 percent, 25 percent, and 15 percent. This was a period in which inflation was brought under control and investors were continually surprised at the changes. Even averaging this period over 20 years would still have this period dominate the estimate of expected returns.<sup>4</sup>

As a second example, the Japanese stock market had a rise of 20 percent per year from 1980 to 1990 as the Japanese economy continued to grow faster than people expected. A series of papers show how historical data could be used to select an international portfolio that dominates holding only a U.S. portfolio since any use of historical data would overweight Japan and lead to high future returns. Likewise, international asset pricing tests have trouble if Japan is included given its large realized return and relative independence from the world market.

What are we to do? One answer is to try to remove the  $I_t$ 's by observing the announcement and

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For those who view return as stationary and that this is a sampling problem I note that the highest previous

adjusting for the surprise. Alternatively, we could develop econometric techniques for identifying the  $I_t$  without observing the announcement and then eliminating it. A different direction is to try to build expectations directly into our asset pricing models. The very old monograph by Meiselman (1962) was a very interesting attempt in this direction. Papers by Fama and Gibbons (1984) and Froot (1989) have some relationship to what I have in mind. Finally, we could test models by seeing if they provide a useful tool for decision making. Pastor and Stambaugh (1999) have made an attempt in this direction. To illustrate these ideas in more detail, it is useful to examine government bond returns.

#### II. The Data

This section describes the data set used in the empirical analysis: the GovPX bond price data and the MMS forecast survey data.

#### A. Price Data

The data set used to calculate expected returns is provided by GovPX. The data set we used contains bid and ask quotes, the price of the last trade as of 3.00 or 6.00 p.m. EST, and trading volume in the inter-dealer broker market for all Treasury bills, notes, and bonds. The data set

return was 16 percent. What are the odds of getting these returns with the historical distribution.

covers the period from July 1, 1991 through December 31, 1997.<sup>5</sup>

The cash market for Treasury securities is much more active than the futures market. For example, during March to May 1993, dealer transactions in the futures market are only about 18 percent of the volume in the cash (Federal Reserve Bulletin (1993)). Likewise, within the cash market the majority of the trades are in the inner market i.e., trades among dealers. According to the same Federal Reserve Bulletin, roughly 62 percent of the March to May 1993 Treasury security transactions in the secondary market occurred within the inner market. Treasury dealers trade with one another mainly through intermediaries, called inter-dealer brokers. Six of the seven main inter-dealer brokers, representing approximately 75 percent of all quotes and a much higher percentage for the maturities we examine, provide price information to the firm GovPX. In turn, GovPX provides price, volume, and quote information to all of the Treasury bond dealers and to other traders through financial news providers, such as Bloomberg.

Dealers leave firm quotes with the brokers, and GovPX shows the best bid and ask for each bond along with the largest size the quote is good for. Thus, the posted quotes are also the prices at which actual trading takes place.<sup>7</sup>

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The time is 6.00 p.m. for data up to Sept. 1996, and 3.00 p.m. for data beyond that date.

The exception is Cantor Fitzgerald. They deal almost exclusively at the long end. Thus, the percentage of all quotes present in the GovPX data for the range of maturities we are examining is much higher than 75 percent.

<sup>&</sup>lt;sup>7</sup> See Balduzzi, Elton, and Green (1998) for a more detailed description of the GovPX data and Elton and Green (1998) for a discussion of its accuracy relative to other sources.

#### B. Survey and Announcement Data

The data on economic announcements and expectations are from Money Market Services (MMS), a San Francisco-based corporation which has conducted telephone surveys since late 1977. The MMS data are the most commonly used expectational data in studies of economic announcements. Balduzzi, Elton, and Green (1998), Edison (1996), Hakkio and Pearce (1985), Ito and Roley (1991), Hardouvelis (1988), McQueen and Roley (1993), and Urich and Wachtel (1984) are some of the many studies that have used the MMS data. The MMS data shows the median forecast, the magnitude of the actual announcement, and the time of the announcement. Thus the error in the consensus forecast can be calculated as well as the exact time this error was known by the market.

#### **III.** Getting Expected Return

In order to obtain estimates of expected return, we first need to construct a realized return series.

The return series needed is returns on zero coupon bonds of different maturities. Using zero

<sup>8</sup> See Balduzzi, Elton, and Green (1998) for a more detailed discussion of the properties of this data.

During the budget crisis at the end of 1996, surveys were not undertaken for two variables. Thus, we do not have errors on one date for two variables. This is an insignificant omission.

We exclude bonds that have not traded for a while, flower bonds, inflation linked and callable bonds, and any bond with a large pricing error.

coupon bonds means that each return is attributed uniquely to a specific maturity. We estimate prices of zero coupon bonds. Each day we estimated the term structure of spot rates by running a cubic spline as described in Elton and Green (1998). With the GovPX database, the average error in price is about 10¢ per \$100 and is random across time and maturity. The term structures are estimated using the last trade price for most bonds in the database. We then calculate the price of a zero coupon bond with maturities of six months, one year, 18 months, and so on up to five years. Daily returns are then computed by taking the log of the price relatives for adjacent days. 11

Bond prices should adjust because of new information that enters the market or because of buying or selling pressure caused by inventory adjustment of financial intermediaries. Insofar as the price changes reflect inventory adjustment, the price changes should be temporary as arbitrageurs take positions reflecting market beliefs about long-term prices. Thus inventory adjustments should introduce random noise and the price changes, separate from the effect of announcement surprises, should be unbiased estimates of expected returns.

We purge the data of announcement effects by removing the estimated effect of the announcement surprises from the daily returns. The superior way to do this would be to remove the information effect by using return data in the fifteen minutes around the announcement. Balduzzi, Elton, and Green (1997) show that all information effects are reflected in the price within this time span. Unfortunately, we do not have intra-day trade data for our full sample

Obviously, after one day the bond has one less day to maturity and this is adjusted for.

period. Our compromise is to use daily data and only the announcements that Balduzzi, Elton, and Green have shown to be important. While we place no reliance on the relative coefficients across announcements given that multiple announcements occur on the same day and that surprises across announcements are correlated, the effect on daily return should be reasonably well estimated. The variables used are surprises in the announcement of the Consumer Price Index, Durable Goods Orders, Housing Starts, Initial Jobless Claims, Non Farm Payrolls, Producers Price Index, Retail Sales, Capacity Utilization, Consumer Confidence, NAPM index, New Homes Sales, and M2 medians. The column labeled expected return in Table I shows the realized return with the effect of announcements removed. The returns are percentage returns for bonds with maturities at six-month intervals up to five years over our full sample period. This is our best estimate of expected return using realized returns. Also included in Table I is the R<sup>2</sup> of the regression of realized returns on announcements.<sup>12</sup> The returns are annualized. Information surprises in economic announcements have little effect on the return for short maturity bonds. For bonds of maturities from one to five years, there is significantly more impact, and removing the effect of announcements has a real impact on the time series of returns. 13 Most of the equilibrium models in the bond area are continuous time models so that it seems most appropriate to examine what happens to daily returns rather than returns over longer intervals. To examine

Balduzzi, Elton, and Green found that several announcements accounted for over 50 percent of the within day volatility. We find a much lower R<sup>2</sup>. We are explaining daily volatility and many days do not have announcements.

The are a whole lot of issues that I have ignored. These concern how well the median of the forecast measures the expected announcement, errors introduced because of imperfect measurement, and the best structural form for the effect of the announcement on return.

the difference that the adjustment makes, I calculate on each announcement day the absolute difference between the adjusted and the raw returns and scale it by the mean absolute unadjusted return. For more than 75 percent of the days, the percentage difference is more than 20 percent, for 40 percent of the days it is more than 40 percent, and for 20 percent of the days, it is more than 60 percent. As shown in Table I, the adjustment also affects the standard deviation of daily returns. Furthermore when we remove the effect of information surprises, kurtosis which is significant for the unadjusted data is no longer significant.

#### IV. Tests in the Bond Area

Modern bond research views bond returns as composed of a return common to all bonds that reflects the return due to the passage of time and a risk premium for bearing term structure risk. Generally, empirical evidence and modern bond pricing theory suggest that the risk premium changes over time as a function of state variables, but we do some preliminary tests assuming a constant term premium.

#### A. A Constant Risk Premium

If the risk premium is constant, then the expected return should equal the one-month interest rate plus a term premium related to the maturity of the bond. If term premiums are defined per period rather than over the full life of the bond, then the difference between a bond's return (with the

effect of surprises removed) and the riskless rate is simply the one period term premium for that maturity bond. In equation form this is

$$R_{it} - R_{Ft} = P_{it} \tag{3}$$

where  $R_{it}$  is the return on a bond of maturity i in period t with the effect of information surprises removed,  $P_{it}$  is the  $t^{th}$  period term premium for a bond of maturity I,  $R_{Ft}$  is the riskless rate in period t.

If term premiums are constant over time then a simple average of the monthly excess returns should provide an estimate of it and the  $i^{th}$  term premium is  $\overline{P}_i = \sum P_{it} \ / \ T$ .

Table II shows the estimate of the term premium assuming a constant term premium over the period from July 1991 to December 1997. As the riskless rate we use the return on a constant maturity one month bill.<sup>14</sup> The estimates of the term premium are generally positive and increase in maturity.

One of the implications of the generalized expectations theory is that forward rates are expected future spot rates plus term premiums. It is useful to examine how term premiums estimated from forward rates compare to the term premiums just calculated.

The definition of the term premium is slightly different here. In this case, it is the premium over the full

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A very similar method of estimating risk premiums is to regress excess return on surprises and use the intercept as the estimate of the risk premium. Since one does not expect correlation between the riskless rate and the surprises this is equivalent to the procedure just described.

#### B. Forward Rates and Risk Premiums

If we let F represent forward rates, then 15

$$F_{t,t+1,t+J} = \sum_{K=t+1}^{t+J-1} \overline{R}_{J-K,K} + P_{J-t-1,t+1}$$
(4)

where  $F_{t,t+1,t+J}$  is the forward rate from t+1 to t+J as of time t, and the bar indicates expected value.

Rearranging we have

$$P_{J-t-1,t+1} = F_{t,t+1,t+J} - \sum_{K=t+1}^{t+J-1} R_{J-K,K}$$
 (5)

The estimates of annualized term premiums using forward rates are contained in Table III. Note that estimates of the term premium using forward rates have the same pattern of increasing with maturity as those obtained earlier and at least at the long end have the expected magnitude. One way to examine the reasonableness of the constant risk premiums is to see if they are related to factors that explain the structure of returns over time. To examine this, we initially need to examine what factors effect government bond returns.

### C. Factor Analysis

period. Thus, these premiums should be averages of those shown in Table II.

To get an idea of the return structure, we factor analyze the variance/covariance matrix of returns. There is some history of this in bond research (see Elton, Gruber, and Michaely (1990) and Litterman and Scheinkman (1991)). Both papers factor analyze the return series on couponpaying bonds. Since the return on a coupon bond is a weighted average of returns on zeros using the return on coupon bonds induces correlation among bond returns even when there would be none if returns on pure discount bonds were used. Therefore, we perform a maximum likelihood factor analysis on the daily return series of the pure discount bonds. In this case we use the daily return series with the effect of surprises included. Since the biggest changes are likely to be associated with surprises, this gives us a better chance of uncovering the structure. After factor analyzing the series, we then regress each return series three months, six months, one year, etc. on the factors. Table IV shows the adjusted R<sup>2</sup> of a regression of returns of the various maturity zeros on factor portfolios for one to four-factor solutions. The first factor captures much of the return pattern for bonds that have a maturity of two years or more. 16 Examining the composition of the first factor shows that it is one-third in the three-year bond and about 10 percent in each of the six bonds closest to it. Examining R<sup>2</sup> for the shorter maturity bonds shows that they seem to move independently of the longer maturity. When a second factor enters the R<sup>2</sup> for the longer maturity bonds hardly changes. However, including two factors causes the R<sup>2</sup> on the short end to

The lower explanatory power on the five year bond is caused by a poor fit of the spline for the long end on a few dates. The poor fit causes a high return on one date and a large negative return on the adjacent one and causes returns to be poorly aligned on a couple of dates.

jump dramatically. Examining the composition of the second factor, it is exclusively the six-month bond. This suggests again that the returns on bonds of different maturities are affected by at least two factors. The last column shows the explanatory power for a pre-specified two-factor model where the two factors are the return on the four-year and six-month bond. The factor analytical solution must better explain the return pattern in sample; but having recognized this, the pre-specified two factors do almost as well. Whether a third factor is important is unclear. It leads to some improvement and some deterioration. Examining the composition of the factor shows that it is generally long the short maturity bonds and short the long maturities, with the heaviest weights being in the one and one-half and four-year bonds. However, the pattern is not monotonic, suggesting that it is primarily picking up idiosyncratic return. When we introduce four or more factors, the composition of the factor is heavily weighted in one maturity, indicating that two or three factors capture everything systematic.

What are these factors? One thing they are not is related to characteristics of the one month rate. For example, regressing the three factors on volatility of the one month rate shows no significance. Looking at the composition of the factors suggests they are a short rate and a long rate. Regressing the two factors on the four-year and six-month bond produces  $R^2$  of 0.94 and 1.0 (since one factor is the six-month bond).

Theory suggests that what matters are the factors that are common across asset categories; after all major investors hold all categories of assets. Asset pricing models in the bond area and the common stock area have developed almost completely independently. In the common stock area the asset pricing model is derived either from the efficiency of some portfolio or from an assumed return-generating process where the factors in the return-generating process are portfolios. In the bond area the fundamental building block is usually an interest rate series. It is unusual for anyone testing in one area to use results from the other asset class. The few attempts that exist have been primarily adding bonds to the S&P Index or an interest rate factor to a multi-factor return-generating process when testing asset pricing models for common stocks.

To examine if there is a commonality between the bond and stock factors, we regressed our factors extracted from bond returns on the Connor Korajczyk factors derived using principal component analysis from common stocks.<sup>17</sup> The results are shown in Table V. None of the factors that explain government bond returns are related to any of the Connor Korajczyk factors derived from the returns on common equities. This seeming independence very much simplifies the asset allocation decision.<sup>18</sup>

Standard asset pricing theory suggests that expected return should be related to the sensitivity to the factors. If the sensitivity is unchanged over time, then expected return should be linearly related to the factor loadings. To test this, we employ the standard maximum likelihood ratio test,

Robert Korajczyk generously supplied the monthly factor returns.

A caution is in order. Bond indexes including corporate return series are related to stock returns. See Elton, Gruber, and Blake (1998). The reason for this is likely to be that the term premium on corporates is related stock market factors. See Elton, Gruber, Agrawal, and Mann (1998).

(See Campbell, Lo and MacKinlay (1997)). This test involves comparing the determinant of the variance covariance matrix of the residuals when the intercept of the return generating process is unconstrained and when the intercept is constrained to fit a linear asset pricing model. There is a difficulty with our sample (the Lindley (1957) problem). Since we have so many time series observations relative to the number of different maturities rejection even with no economic significance is highly likely. Therefore, not surprisingly, at standard levels of significance, we can reject the hypothesis that the constrained model is not different from the unconstrained. Examining the variance covariance matrix of the constrained and unconstrained solution and noting that they are identical to the seventh place, suggests that the Lindley problem is serious here. If this is the explanation, then we should observe that the constrained solution (the asset pricing model) yields estimates of expected return that are not different from our estimate in the unconstrained solution and this is the case. Comparing the expected return of the constrained and unconstrained model shows only one difference more than four percent and that difference is 17 percent. Thus, although there is a statistical difference, there is not an economic difference in the constrained and unconstrained solutions and the differences in expected return are explained by differences in sensitivity to the factors.

#### D. Changing Risk Premiums

The evidence on term premiums obtained from examining the relationship between futures rates

and spot rates indicates that term premiums at least for short maturity bonds are changing.<sup>19</sup> The evidence primarily consists of results from regressions of forward rates on one period spots. These results consist of estimates of the slope less than one that remain unexplained by known biases in the estimates.

Modern bond pricing models imply that the risk premium should be changing as a function of maturity and as a function of changes in the level of state variables. Single factor models are particularly easy to analyze.

In a single factor bond pricing model the state variable is normally the short-term rate. In a single factor model like Cox Ingersoll and Ross (1985), the sign of the term premium is not affected by maturity and the magnitude of the term premium is linear in the short rate. Multi-factor models are more complex since the sign of the term premium can change as a function of maturity. In the two-factor model of Longstaff and Schwartz (1992), the magnitude of the term premium is a linear function in the short rate. However, the effect of increases in the short rate on the term premium is less clear. It must always be a positive function for short maturity bonds while the effect of an increase is indeterminate for long maturity bonds. In the Longstaff and Schwartz (1992) model, the second state variable is the variance of the change in the short rate. Once again

See, for example, Backus, Foresi, Mozumdar, and Wu (1997) and Campbell and Shiller (1991). For a different opinion see Froot (1989).

See for example, Brennan and Schwartz (1982). The models can also be expressed as the short rate and a difference in the long and short rate. See Elton, Gruber, and Mei (1996) for an example.

the term premium is linear in the variance, but the sign is indeterminate. The other type of two-factor model examined are models where the state variables are the long and the short rate.<sup>20</sup> In this case the term premium is again linear in the state variables. In general, in all of these models the magnitude of the effect on the term premiums of changes in the state variables decreases with maturity due to mean reversion. Also, in general, the variability of the estimated risk premium increases with maturity. Together these suggest the following regression:

$$R_{it} - R_{Ft} = c_0 + c_1 r_s + c_2 s_s^2 + c_3 r_I + e_{it}$$
 (6)

where  $r_s$  is the short rate,  $r_L$  is the long rate, and  $S_s^2$  is the variance in the change in the short rate.

The expected results are:

- 1.  $c_1$  is non-zero and has the same sign across maturities and the change across maturities is monotonic (single factor CIR)
- 2.  $c_1$  is non-zero and is positive for short maturity bonds, and  $c_2$  is non-zero (Longstaff and Schwartz)
- 3.  $c_1$  and  $c_3$ , are non-zero (Brennan and Schwartz)
- 4. the variance of the residual increases with maturity.

We need to specify how the variables are calculated. Expected return is as discussed earlier. Like others, we use the one-month rate at the beginning of the month for the short rate. For the long-term bond, we selected the spot rate on the five-year bond at the beginning of the month. Finally, for the estimate of the variance of the change in the one-month rate we follow Longstaff and Schwartz (1992) and estimate it using the following GARCH process:

$$\mathbf{r}_{\text{Ft+1}} - \mathbf{r}_{\text{Ft}} = \boldsymbol{a}_0 + \boldsymbol{a}_1 \mathbf{r}_{\text{Ft}} + \boldsymbol{a}_2 \mathbf{V}_{\text{t}} + \boldsymbol{d}_{\text{t+1}}$$

where

$$\boldsymbol{d}_{t+1} = \mathbf{N}(0, \mathbf{V}_t)$$

and

$$V_{t} = \boldsymbol{b}_{0} + \boldsymbol{b}_{1} R_{Et} + \boldsymbol{b}_{2} V_{t,1} + \boldsymbol{b}_{3} \boldsymbol{d}_{t}^{2}$$
 (7)

The results of the regression are shown in Table VI. The one-month rate and the variance of the one-month rate are insignificant for all maturities. The long rate is significant for one and a half to four and a half years. These results suggest that if risk premiums do change, it is not due to changes in the characteristics of the one-month rate. There is some evidence that suggests the long rate might serve as a state variable proxy.

As discussed above, most bond pricing models have focused on characteristics of the short rate as at least one of the state variables, and often in two-factor models, both state variables. I have always thought this was a misplaced emphasis. It seems to me that what permanently shifts the term structure is changes in the information set. Further, there is a general belief among traders

that the short term end of the curve is anchored by Federal Reserve actions and that long rates change because of changes in beliefs about the general state of the economy (which may predict future short rates). This is supported by the work in Balduzzi, Elton, and Green (1997). In this article we look at price reactions to major surprises associated with announcements of economic variables. We find that inclusion of the return on the short bond in a regression of a long bond return on surprises does not change the effect of surprises on long bond returns, while the inclusion of any intermediate or long bond captures the effect of information surprises on other long bonds. Thus the effect of information surprises on long bonds is captured by the return on a long bond, but not the return on a short bond. Likewise, inclusion of the return on a long bond does not capture the information effects on short bonds. It is hard to understand how the level or variability of the short rate captures sensitivity on the long end when the short rate does not seem to react to the same surprises and in the same way as the long rate.<sup>21</sup>

#### V. Asset Pricing Tests in the Common Stock Area

Asset pricing in the common stock area has universally involved using realized returns as a proxy for expected returns. Testing generally takes one of three forms. First is the time series testing where sensitivities and risk premiums are simultaneously estimated and the principal tests involve examining the change in explanatory power of the regression constrained to conform to the pricing model relative to the unconstrained regression. Second, is the two-pass procedure where

In an earlier version of this paper, Balduzzi, Elton, and Green (1997b) found considerable movement in the short rate when the Federal Reserve Board made major changes with no corresponding reaction in long rates.

sensitivities are first estimated and then risk premiums are estimated and the principal test involves the reasonableness of the estimates of the premiums. Both of these tests can be done conditionally where sensitivities or premiums or both are allowed to be time varying. The third procedure is the test of the efficiency of the market portfolio. As shown in Campbell, Lo, and MacKinlay (1997), the first and third procedure are essentially the same. The problem with using realized returns as a proxy for expected returns is prevalent in all three tests. The nature of this problem is easiest to understand with the third test. The test for the efficiency of the market portfolio involves the distance between the market portfolio and the efficient frontier.

Gibbons Ross and Shanken (1989) show that the test of the efficiency of the market portfolio depends on the Sharpe ratio. Knowing this helps us focus on how using realized returns as a

$$R_{it} - R_{Ft} = a_i + \sum b_{ii}^{u} I_{it}^{u} + \sum b_{ii}^{p} I_{it}^{p} + e_{it}$$
 (8)

proxy for expected returns impacts the tests. Consider a general multi-factor model

Where  $\boldsymbol{a}_i$  is the non-index related return,  $R_{it}$  is the return on stock i in period t,  $R_{Ft}$  is the return on the riskless rate in period t,  $\boldsymbol{b}_{ij}$  is the sensitivity of stock i to factor j,  $I_{jt}^P$  is the excess return on a priced factor j,  $I_{jt}^u$  is the excess return on an unpriced factor j, and  $e_{it}$  is the random error term.

There are three ways that information surprises can effect the returns on security i.

1. an unanticipated firm specific announcement where the impact is reflected in  $a_i$ .

- 2. an unanticipated announcement that effects a priced index so that  $I_J^P$  is different than expected
- 3. an unanticipated announcement that effects an index in the return generating process but is not priced so that  $I^u_j$  is nonzero over the period being analyzed when its expected value is zero.

As we see shortly, unanticipated information surprises affect the tests of the reasonableness of the asset pricing model and tests for the number of factors. Each is discussed in turn.

#### A. Information Surprises and Tests of a Particular Asset Pricing Model

We know that if a multi-index model describes the variance covariance structure of returns and there are no unique returns on securities then the efficient frontier can be constructed from a linear combination of the portfolios that replicate the indexes. Likewise, the market portfolio is a linear combination of the replicating portfolios and therefore the market is efficient. Whether the return on all factors is expected return or there are large information surprises that cause realized return to be different from expected returns for these indexes does not affect the efficiency of the market portfolio. What does cause the market portfolio to be interior is information surprises about individual companies or missing indexes whether priced or not. Both of these cause a non zero alpha on individual securities and cause the market to be interior.

What can be learned by realizing that the test involves comparison of Sharpe ratios? The presence of large informational surprises has two impacts on the Sharpe ratio. First, the larger the alpha, the greater the shift in the ratio and the more interior is the market. However, the increased alpha causes greater concentration and an increase in the denominator. However, the impact on the numerator will likely be much larger than the impact on the denominator. This follows because: The likely effect of having securities with alphas is to have the portfolio weights be more concentrated in a few securities. Greater concentration has the same effect on portfolio variance as having fewer securities in the portfolio. However, the effect on variance as the number of securities in the portfolio increases is fairly modest for reasonable size portfolios. Thus what is most important for changing the Sharpe ratio and rejecting the asset pricing model is a few large information surprises which have the impact of substantially increasing the numerator with little impact on the denominator, rather than a lot of securities with small surprises which have much less impact on the numerator and essentially no impact on the denominator.

What do we learn from this discussion? If we are using individual company returns, we are likely to get a substantial number of large surprises as the number of securities increases and always reject the asset pricing model with a high probability. What sort of information events might cause a substantial alpha for an individual security. Corporate restructuring such as being acquired is likely to be associated with a large alpha. An announcement of a successful new product or discovery such as a drug or oil field or the announcement of a failure to develop a long anticipated product is likely to be associated with a large alpha. Major earnings surprises would also likely be

associated with a large alpha. In short, any announcement that would substantially change the markets perception of the future earning power of the firm would likely have a large alpha associated with it.

To get an idea of whether information surprises alone could lead to rejections of an asset pricing model using individual securities, I perform two simulation experiments. I assume a single factor asset pricing model held exactly so that all alphas are zero absent information surprises. I then superimpose information surprises on the pricing model. The first information surprise I select is earnings. I calibrate the surprise to match the empirical findings of Bernard and Thomas (1990). If I assume a normal distribution then I find a mean of zero and a standard deviation of 0.38 which matches the effect of the quarterly earnings surprise that they found. I assume that the earnings announcements are independent through time. For 10 year intervals, I calculate the distribution of surprises (how many positive and negative surprises). For simplicity, I assume that the negative and positive surprises cancel out, thus I use the net number of surprises in calculating alpha. If alpha is normally distributed with a mean of zero and standard deviation of 0.38 and surprises in announcements are independent, then the impact on alpha has a mean of zero and standard deviation 0.38 times the square root of the number of surprises that don't cancel out. As shown in Gibbons, Ross, and Shanken (1989), the test statistic of whether the constrained model cannot be rejected is a F test with N degrees in the numerator and T-N-1 in the denominator and is equal to

$$\frac{T-N-1}{N} \left[ 1 - \frac{r_M}{s_M^2} \right]^{-1} a' \sum_{i=1}^{N} a'$$

and

$$\sum a' \sum^{-1} a = \frac{\overset{-2}{r_P}}{\overset{-2}{s_P^2}} - \frac{\overset{-2}{r_M}}{\overset{2}{s_M}}$$
(9)

where  $\bar{r}$  is mean return,  $\boldsymbol{s}$  is standard deviation, the subscript M is market, the subscript P is the sample portfolio, T is number of time periods, N is number of securities,  $\boldsymbol{a}$  is a vector of alphas, and  $\sum$  is the variance covariance matrix

I select an annual  $\bar{r}_M$  equal to eight percent and  $\boldsymbol{s}_M^2$  equal to 20 percent roughly matching historical numbers.<sup>22</sup>

The probability of rejecting the asset pricing model due to the information surprise given sample sizes of 10 to 100 securities varies from four percent to 18 percent. This is substantial. The second simulation assumes a discrete distribution of surprises. I select 500 stocks at random and compute the number of times daily return exceeds one percent, two percent, etc. or minus the same, conditional on this return being more than three times the market. Since betas of  $\pm 3$  are not plausible, this seems to be a good measure of surprises, although it does control for non-market factors. Then, for each firm, I sum the surprises over 10 years. The distribution of annualized 10 year surprises is shown in Table VII. Once again, I draw observations from this distribution for

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 $<sup>^{22}</sup>$  For simplicity, I assume a market model holds and standard deviations on all assets are the same. I use a

different size portfolios and compute rejection probabilities. The rejection due to information surprises varies from one to 95 percent. Thus, information surprises for individual securities lead to substantial rejection of the asset pricing model even when it's true.

It is difficult to remove information surprises from individual company returns by examining individual announcements for firms. Perhaps statistical techniques can be developed here. Grouping is another way to mitigate the effect of information surprises on individual securities. There is, of course, a danger in grouping. Misspecified asset pricing models lead to large alphas and these should be correctly rejected. The grouping criteria involve attempting to average out information surprises and an attempt to not average out non-zero alphas caused by a misspecified model. This is likely to require careful thought about alternative models. Obviously we need to be careful that we don't group on a criteria that implicitly groups on the basis of the sign and size of the information surprise. For example, if the information surprises are correlated across securities such as commodity price shocks, then the grouping has to be careful to diversify across firms that have different exposures to the shock. Likewise, using country returns and grouping by country is a problem since the information surprise like market movements or exchange rate changes will likely impact all securities in a country. An information surprise that affects a sector such as an oil price shock can be eliminated by introducing an index capturing the shock to the return-generating process. This leads to a reduction in the non-zero alphas and if the information shock is substantial appears as a priced factor whether it is or is not.

simplified version of Elton, Gruber, and Padberg (1976) to calculate security proportions.

#### **B.** Number of Priced Factors

Now let us consider a factor that is in the return generating process but is not priced. Also assume there is a large information shock or a number of shocks in the same direction. If the security specific returns are all zero, and the return generating process includes all the factors, then the asset pricing model would not be rejected but the factor price on the unpriced factor would likely appear non zero and would be determined by the information surprise. The impact of leaving out an unpriced factor from the return-generating process is likely to be worse. Again, in any sample period information surprises are likely to mean that the factor has a non-zero return and the intercept with the factor left out is equal to the product of the sensitivities times the information surprise. If some sensitivities are large, positive or negative, this causes large alphas. Thus the asset pricing model is rejected. A factor should be priced for one of two reasons. First, if investors are mean variance maximizers and sensitivity to the factor ex ante affects mean returns. Second, it is priced because sensitivity to it satisfies a hedging demand either because of a changing consumption set (see Merton (1969)) or in one period context because investors care about sensitivity to it. Let's consider inflation as an example. Assume unanticipated inflation surprises do not meet a hedge demand. Then inflation will be priced if investors are mean variance maximizers in real returns since inflation will ex ante affect mean real returns. If investors are mean variance maximizers in nominal returns then inflation should not be priced even if it's part of the return generating process. If it serves a hedge demand, then it also should be priced.<sup>23</sup>

<sup>&</sup>lt;sup>23</sup> This distinction and the assumptions underlying different asset pricing models that incorporate inflation are

There should be lots of factors in the return generating process that are useful in explaining covariance but do not serve any hedge demands nor affect expected returns. It is likely that there will be information surprises in these factors and that the sample mean will be significantly non zero in many periods. Thus it is difficult to separate out whether it is an unpriced factor or risk premiums are changing over time. However, this is an area where the techniques discussed with reference to bonds may well be relevant. While it is likely to never be possible to control for information surprises for individual company events, it may well be possible to control for information surprises in factors if these factors are economic variables. One test for priced factors is to look at the excess return on the factor replicating portfolios (see Balduzzi and Kallal (1997)). Consider again a factor like inflation. The realized return on the factor replicating portfolios will be heavily influenced by the unanticipated announcements concerning inflation. However, these could be identified and return on days of information surprises could be eliminated or the effect of the surprise controlled for.

#### C. Implications

First, grouping should be part of any tests using current methodology. One reason for grouping is to eliminate company-specific surprises. In deciding on a grouping procedure, this purpose should have a dominant role. Second, traditional testing is likely to overstate the number of priced

discussed in Elton and Gruber (1983).

factors. Insight into which factors could be priced are likely to come as much from theory as from empirical results. Inflation is a useful example. Generally we believe that investors should look at real returns in making their investment decisions. Thus there is a lot of theory that suggests inflation sensitivity is important in affecting investors hedging demands and should be priced. Now consider momentum. Accept for a moment the empirical evidence that momentum is related to realized returns. If there is any connection between momentum and changes in the opportunity set, I am not aware of it. Thus momentum is the kind of factor that is likely to appear in the return-generating process and likely to appear priced in sample but for which there is no theory that would suggest that it should be priced and for which current testing procedures are unlikely to be helpful.

#### **Summary**

When I first entered the Profession, anyone using realized returns as expected returns made the argument that in the long run we should get what we expect. Even this weak defense is no longer used and researchers generally treat realized returns as expected returns in their tests without any qualifications. The purpose of this article is to convince the reader there is a distinction and that it is worth our collective efforts to think about alternative ways to estimate expected returns. I have tried to examine some alternatives. I do not pretend that I have the final answers here. However, I do hope that I have convinced you that it is a worthwhile search.

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## Table I Estimates of Expected Returns

This table shows the results of regressions of daily realized returns on important information surprises for that day. One regression is run for each maturity listed below over the full sample period (July 91 to December 97). Expected Return is the estimate of the intercept in this regression, expressed as an annualized percentage. Adjusted  $R^2$  of the regression represents the impact of surprise removal from realized returns.

Maturity	Expected Return	Adjusted $R^2$
1 month	3.095%	0.004
6 months	3.575%	0.105
1 year	4.053%	0.154
1.5 years	4.395%	0.151
2 years	4.675%	0.147
2.5 years	5.070%	0.136
3 years	5.493%	0.132
3.5 years	5.808%	0.126
4 years	6.013%	0.122
4.5 years	6.312%	0.116
5 years	5.925%	0.081

# Table II Estimates of Term Premiums

This table shows the estimates of term premiums, computed as the average over the sample period of the difference between the Expected Returns on the bonds of a given maturity and the riskless rate. The Expected Returns on bonds were constructed by removing the effect of information surprises from the realized returns. Returns on a constant maturity one month bill are used for the riskless rate. The premiums are in annualized percentages.

Premium		
0.471%		
0.937%		
1.272%		
1.547%		
1.935%		
2.352%		
2.660%		
2.855%		
3.143%		
2.795%		

# Table III Estimates of Term Premiums using Forward Rates

This table shows the estimates of term premiums computed as the difference of the forward rate and the expected future spot rate. The expected future spot rates are computed by summing the expected future returns, as in equation (2). The premiums are in annualized percentages.

Maturity	Premium
6 months	1.412%
1 year	1.581%
1.5 years	1.730%
2 years	1.890%
2.5 years	2.046%
3 years	2.183%
3.5 years	2.268%
4 years	2.288%
4.5 years	2.283%

Table IV Explanatory Power of the Factors

This table shows the Adjusted  $R^2$  in the regression of returns on factor portfolios for one to four factor solutions. The last column shows the explanatory power of a pre-specified two factor model where the two factors are the returns on the six month and four year bonds.

Maturity	One Factor	Two Factors	Three Factors	Four Factors	Pre-Specified
					Two Factors
1 month	0.012	0.406	0.450	0.551	0.352
6 months	0.472	1.000	1.000	1.000	1.000
1 year	0.831	0.908	0.971	0.987	0.860
1.5 years	0.905	0.916	0.981	0.994	0.852
2 years	0.962	0.965	0.984	0.989	0.888
2.5 years	0.953	0.955	0.944	0.999	0.871
3 years	0.987	0.985	0.977	0.977	0.907
3.5 years	0.970	0.966	0.976	0.969	0.942
4 years	0.942	0.940	0.976	0.988	1.000
4.5 years	0.917	0.916	0.951	0.970	0.959
5 years	0.599	0.599	0.604	0.616	0.608

Table V Relationship between the bond factors and the stock factors

This table shows the results of regression of bond factors (extracted by factor analysis) on the Connor-Korajczyk stock factors (*ck1* to *ck5*). Abbreviations *1-FM*, *2-FM* and *3-FM* stand for One Factor Model, Two Factor Model, and Three Factor Model respectively. Numbers in parentheses are *t*-statistics.

Model	Factor	Constant	ck1	ck2	ck3	ck4	ck5	$R^2$
1-FM	fl	-2.82	259.52	38.61	326.38	-58.44	-199.01	0.011
		-(0.35)	(0.89)	(0.19)	(2.02)	-(0.35)	-(1.11)	
2-FM	fI	-1.19	73.11	-7.74	42.49	-8.91	-36.27	0.000
		-(0.70)	(1.19)	-(0.18)	(1.25)	-(0.25)	-(0.96)	
	f2	-2.91	263.99	38.89	332.02	-59.26	-204.02	0.010
		-(0.35)	(0.88)	(0.19)	(2.01)	-(0.34)	-(1.11)	
3-FM	fI	-1.19	73.11	-7.74	42.49	-8.91	-36.27	0.000
		-(0.70)	(1.19)	-(0.18)	(1.25)	-(0.25)	-(0.96)	
	f2	-2.96	256.09	32.37	320.83	-60.93	-203.33	0.008
		-(0.36)	(0.86)	(0.16)	(1.96)	-(0.36)	-(1.11)	
	f3	-13.55	-522.19	-685.94	-699.69	-119.39	-370.25	-0.028
		-(0.38)	-(0.40)	-(0.76)	-(0.96)	-(0.16)	-(0.46)	

Table VI Sensitivities of Term Premiums to State Variables

This table shows the results of the regression:  $R_{it}$  -  $R_{Ft} = C_0 + C_1 r_s + C_2 s_s^2 + C_3 r_L + e_{it}$ , where  $r_s$  is the short rate,  $r_L$  is the long rate and  $s_s^2$  is the variance of the short rate. Numbers in parentheses are the t-statistics.

Maturity	$C_0$	$C_I$	$C_2$	$C_3$	Adjusted $R^2$
1 month	0.003	-0.246	11.256	-0.099	0.428
	(1.05)	-(5.08)	(0.29)	-(1.63)	
6 months	-0.016	-0.151	82.109	0.205	-0.013
	-(1.46)	-(0.92)	(0.62)	(0.99)	
1 year	-0.059	-0.147	320.479	0.902	0.021
	-(2.14)	-(0.36)	(0.97)	(1.75)	
1.5 years	-0.110	-0.190	522.438	1.763	0.038
	-(2.37)	-(0.27)	(0.94)	(2.02)	
2 years	-0.156	-0.246	598.096	2.567	0.041
	-(2.40)	-(0.25)	(0.77)	(2.10)	
2.5 years	-0.196	-0.351	656.175	3.338	0.042
	-(2.38)	-(0.29)	(0.67)	(2.16)	
3 years	-0.242	-0.545	863.549	4.236	0.047
	-(2.43)	-(0.37)	(0.72)	(2.26)	
3.5 years	-0.287	-0.755	1054.509	5.111	0.050
	-(2.44)	-(0.43)	(0.75)	(2.31)	
4 years	-0.319	-0.897	1078.575	5.750	0.044
	-(2.35)	-(0.44)	(0.66)	(2.26)	
4.5 years	-0.351	-0.896	1167.716	6.301	0.045
	-(2.37)	-(0.40)	(0.66)	(2.26)	
5 years	-0.370	-1.002	820.403	6.716	0.031
	-(2.18)	-(0.39)	(0.40)	(2.10)	

## Table VII Frequency Distribution of Surprises

This table shows the empirical distribution of information surprises. Five hundred common stocks were randomly picked up from the universe of NYSE listed stocks with returns data in the ten year period from 1986 to 1995 taken from CRSP files. If any return is greater than one percent (in magnitude) and greater than three times the market return (in magnitude), it was treated as an information surprise for that stock. All such surprises for a stock are cumulated over the 10 year period to find the total net surprise. The total net surprise over 10 years is divided by 10 to get the annualized surprise. The range shown in the table below is for a total of 500 annualized surprises.

Range	Frequency*
-50% to -25%	2
-25% to 0%	179
0% to 25%	238
25% to 50%	64
50% to 75%	12
75% to 100%	2
100% to 125%	1
125% to 150%	1
150% to 175%	0
175% to 200%	1