VALUATION: PACKET 3
REAL OPTIONS, ACQUISITION
VALUATION AND VALUE ENHANCEMENT

Aswath Damodaran
Updated: January 2022
REAL OPTIONS: FACT AND FANTASY
Underlying Theme: Searching for an Elusive Premium

- Traditional discounted cashflow models underestimate the value of investments, where there are options embedded in the investments to:
  - Delay or defer making the investment (delay)
  - Adjust or alter production schedules as price changes (flexibility)
  - Expand into new markets or products at later stages in the process, based upon observing favorable outcomes at the early stages (expansion)
  - Stop production or abandon investments if the outcomes are unfavorable at early stages (abandonment)

- Put another way, real option advocates believe that you should be paying a premium on discounted cashflow value estimates.
A bad investment...

Today

Success 1/2

+100

Failure 1/2

-120

Aswath Damodaran
Becomes a good one...
Three Basic Questions

1. When is there a real option embedded in a decision or an asset?
2. When does that real option have significant economic value?
3. Can that value be estimated using an option pricing model?
When is there an option embedded in an action?

- An option provides the holder with the right to buy or sell a specified quantity of an underlying asset at a fixed price (called a strike price or an exercise price) at or before the expiration date of the option.
- There has to be a clearly defined underlying asset whose value changes over time in unpredictable ways.
- The payoffs on this asset (real option) have to be contingent on a specified event occurring within a finite period.
Payoff Diagram on a Call

Price of underlying asset

Strike Price

Net Payoff on Call

Price of underlying asset
Payoff Diagram on Put Option
When does the option have significant economic value?

- For an option to have significant economic value, there has to be a restriction on competition in the event of the contingency. In a perfectly competitive product market, no contingency, no matter how positive, will generate positive net present value.

- At the limit, real options are most valuable when you have exclusivity - you and only you can take advantage of the contingency. They become less valuable as the barriers to competition become less steep.
Determinants of option value

- Variables Relating to Underlying Asset
  - Value of Underlying Asset: as this value increases, the right to buy at a fixed price (calls) will become more valuable and the right to sell at a fixed price (puts) will become less valuable.
  - Variance in that value: as the variance increases, both calls and puts will become more valuable because all options have limited downside and depend upon price volatility for upside.
  - Expected dividends on the asset, which are likely to reduce the price appreciation component of the asset, reducing the value of calls and increasing the value of puts.

- Variables Relating to Option
  - Strike Price of Options: the right to buy (sell) at a fixed price becomes more (less) valuable at a lower price.
  - Life of the Option: both calls and puts benefit from a longer life.

- Level of Interest Rates: as rates increase, the right to buy (sell) at a fixed price in the future becomes more (less) valuable.
When can you use option pricing models to value real options?

- The notion of a replicating portfolio that drives option pricing models makes them most suited for valuing real options where:
  - The underlying asset is traded - this yield not only observable prices and volatility as inputs to option pricing models but allows for the possibility of creating replicating portfolios.
  - An active marketplace exists for the option itself.
  - The cost of exercising the option is known with some degree of certainty.

- When option pricing models are used to value real assets, we have to accept the fact that:
  - The value estimates that emerge will be far more imprecise.
  - The value can deviate much more dramatically from market price because of the difficulty of arbitrage.
The objective in creating a replicating portfolio is to use a combination of riskfree borrowing/lending and the underlying asset to create the same cashflows as the option being valued.

- Call = Borrowing + Buying D of the Underlying Stock
- Put = Selling Short D on Underlying Asset + Lending
- The number of shares bought or sold is called the option delta.

The principles of arbitrage then apply, and the value of the option has to be equal to the value of the replicating portfolio.
The Binomial Option Pricing Model

Option Details

K = $40
t = 2
r = 11%

100 D - 1.11 B = 60
50 D - 1.11 B = 10
D = 1, B = 36.04
Call = 1 * 70 - 36.04 = 33.96

70 D - 1.11 B = 33.96
35 D - 1.11 B = 4.99
D = 0.8278, B = 21.61
Call = 0.8278 * 50 - 21.61 = 19.42

50

Call = 19.42

35

Call = 4.99

50 D - 1.11 B = 10
25 D - 1.11 B = 0
D = 0.4, B = 9.01
Call = 0.4 * 35 - 9.01 = 4.99

25

0

Stock
Price

100
60

70
33.96

50
10

35

25
The Limiting Distributions....

- As the time interval is shortened, the limiting distribution, as \( t \to 0 \), can take one of two forms.
  - If as \( t \to 0 \), price changes become smaller, the limiting distribution is the normal distribution and the price process is a continuous one.
  - If as \( t \to 0 \), price changes remain large, the limiting distribution is the Poisson distribution, i.e., a distribution that allows for price jumps.

- The Black-Scholes model applies when the limiting distribution is the normal distribution, and explicitly assumes that the price process is continuous and that there are no jumps in asset prices.
The version of the model presented by Black and Scholes was designed to value European options, which were dividend-protected.

The value of a call option in the Black-Scholes model can be written as a function of the following variables:

- $S =$ Current value of the underlying asset
- $K =$ Strike price of the option
- $t =$ Life to expiration of the option
- $r =$ Riskless interest rate corresponding to the life of the option
- $\sigma^2 =$ Variance in the In(value) of the underlying asset
The Black Scholes Model

Value of call = \( S \, N(d_1) - K \, e^{-rt} \, N(d_2) \)

where

\[
d_1 = \frac{\ln\left(\frac{S}{K}\right) + (r + \frac{\sigma^2}{2}) \, t}{\sigma \sqrt{t}}
\]

\[d_2 = d_1 - \sqrt{t}\]

- The replicating portfolio is embedded in the Black-Scholes model. To replicate this call, you would need to
  - Buy \( N(d_1) \) shares of stock; \( N(d_1) \) is called the option delta
  - Borrow \( K \, e^{-rt} \, N(d_2) \)
### The Normal Distribution

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Adjusting for Dividends

- If the dividend yield ($y = \text{dividends}/\text{Current value of the asset}$) of the underlying asset is expected to remain unchanged during the life of the option, the Black-Scholes model can be modified to take dividends into account.

- \[ C = S e^{-yt} N(d1) - K e^{-rt} N(d2) \]

  where,

  \[ d_1 = \frac{\ln\left(\frac{S}{K}\right) + (r - y + \frac{\sigma^2}{2}) t}{\sigma \sqrt{t}} \]

  \[ d_2 = d_1 - \sigma \sqrt{t} \]

- The value of a put can also be derived:

  \[ P = K e^{-rt} (1-N(d2)) - S e^{-yt} (1-N(d1)) \]

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Most practitioners who use option pricing models to value real options argue for the binomial model over the Black-Scholes and justify this choice by noting that:

- Early exercise is the rule rather than the exception with real options.
- Underlying asset values are generally discontinuous.

If you can develop a binomial tree with outcomes at each node, it looks a great deal like a decision tree from capital budgeting. The question then becomes when and why the two approaches yield different estimates of value.
The Decision Tree Alternative

- Traditional decision tree analysis tends to use
  - One cost of capital to discount cashflows in each branch to the present
  - Probabilities to compute an expected value
  - These values will generally be different from option pricing model values

- If you modified decision tree analysis to
  - Use different discount rates at each node to reflect where you are in the decision tree (This is the Copeland solution)  
  - Use the riskfree rate to discount cashflows in each branch, estimate the probabilities to estimate an expected value and adjust the expected value for the market risk in the investment

- Decision Trees could yield the same values as option pricing models
A decision tree valuation of a pharmaceutical company with one drug in the FDA pipeline...

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Key Tests for Real Options

- Is there an option embedded in this asset/decision?
  - Can you identify the underlying asset?
  - Can you specify the contingency under which you will get payoff?

- Is there exclusivity?
  - If yes, there is option value.
  - If no, there is none.
  - If in between, you have to scale value.

- Can you use an option pricing model to value the real option?
  - Is the underlying asset traded?
  - Can the option be bought and sold?
  - Is the cost of exercising the option known and clear?
One of the limitations of traditional investment analysis is that it is static and does not do a good job of capturing the options embedded in investment.

- The first of these options is the option to delay taking an investment, when a firm has exclusive rights to it, until a later date.
- The second of these options is taking one investment may allow us to take advantage of other opportunities (investments) in the future.
- The last option that is embedded in projects is the option to abandon an investment, if the cash flows do not measure up.

These options all add value to projects and may make a “bad” investment (from traditional analysis) into a good one.
A. The Option to Delay

- When a firm has exclusive rights to a project or product for a specific period, it can delay taking this project or product until a later date.

- A traditional investment analysis just answers the question of whether the project is a “good” one if taken today.

- Thus, the fact that a project does not pass muster today (because its NPV is negative, or its IRR is less than its hurdle rate) does not mean that the rights to this project are not valuable.
Valuing the Option to Delay a Project

Initial Investment in Project

PV of Cash Flows from Project

Present Value of Expected Cash Flows on Product

Project has negative NPV in this section

Project's NPV turns positive in this section

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Example 1: Valuing product patents as options

- A product patent provides the firm with the right to develop the product and market it.
- It will do so only if the present value of the expected cash flows from the product sales exceed the cost of development.
- If this does not occur, the firm can shelve the patent and not incur any further costs.
- If I is the present value of the costs of developing the product, and V is the present value of the expected cashflows from development, the payoffs from owning a product patent can be written as:

  Payoff from owning a product patent = V - I

  = 0

  if V > I

  if V ≤ I
Payoff on Product Option

Net Payoff to introduction

Present Value of cashflows on product

Cost of product introduction
## Obtaining Inputs for Patent Valuation

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<th>Estimation Process</th>
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<td>1. Value of the Underlying Asset</td>
<td>• Present Value of Cash Inflows from taking project now</td>
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<tr>
<td></td>
<td>• This will be noisy, but that adds value.</td>
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<td>2. Variance in value of underlying asset</td>
<td>• Variance in cash flows of similar assets or firms</td>
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<td>• Variance in present value from capital budgeting simulation.</td>
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<td>3. Exercise Price on Option</td>
<td>• Option is exercised when investment is made.</td>
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<td>• Cost of making investment on the project; assumed to be constant in present value dollars.</td>
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<td>4. Expiration of the Option</td>
<td>• Life of the patent</td>
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<td>5. Dividend Yield</td>
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<td>• Each year of delay translates into one less year of value-creating cashflows</td>
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<td>Annual cost of delay $= \frac{1}{n}$</td>
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Valuing a Product Patent: Avonex

Biogen, a bio-technology firm, has a patent on Avonex, a drug to treat multiple sclerosis, for the next 17 years, and it plans to produce and sell the drug by itself.

The key inputs on the drug are as follows:

- PV of Cash Flows from Introducing the Drug Now = $3.422 billion
- PV of Cost of Developing Drug for Commercial Use = $2.875 billion
- Patent Life = 17 years    Riskless Rate = r = 6.7% (17-year T.Bond rate)
- Variance in Expected Present Values = $0.224 (Industry average firm variance for bio-tech firms)
- Expected Cost of Delay = y = 1/17 = 5.89%

The output from the option pricing model

- $d_1 = 1.1362$    $N(d_1) = 0.8720$
- $d_2 = -0.8512$    $N(d_2) = 0.2076$

Call Value = $3,422 \exp(-0.0589)(17)(0.8720) - 2,875 \exp(-0.067)(17)(0.2076) = $907 million
The Optimal Time to Exercise

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Patent value versus Net Present value

Exercise the option here: Convert patent to commercial product
Valuing a firm with patents

- The value of a firm with a substantial number of patents can be derived using the option pricing model.
  
  \[
  \text{Value of Firm} = \text{Value of commercial products (using DCF value + Value of existing patents (using option pricing) + (Value of New patents that will be obtained in the future – Cost of obtaining these patents) }
  \]

- The last input measures the efficiency of the firm in converting its R&D into commercial products. If we assume that a firm earns its cost of capital from research, this term will become zero.

- If we use this approach, we should be careful not to double count and allow for a high growth rate in cash flows (in the DCF valuation).
Value of Biogen’s existing products

- Biogen had two commercial products (a drug to treat Hepatitis B and Intron) at the time of this valuation that it had licensed to other pharmaceutical firms.
- The license fees on these products were expected to generate $50 million in after-tax cash flows each year for the next 12 years.
- To value these cash flows, which were guaranteed contractually, the pre-tax cost of debt of the guarantors was used:

\[
\text{Present Value of License Fees} = \frac{50 \text{ million} \times (1 - (1.07)^{-12})}{.07} = \$397.13 \text{ million}
\]
Biogen continued to fund research into new products, spending about $100 million on R&D in the most recent year. These R&D expenses were expected to grow 20% a year for the next 10 years, and 5% thereafter.

It was assumed that every dollar invested in research would create $1.25 in value in patents (valued using the option pricing model described above) for the next 10 years, and break even after that (i.e., generate $1 in patent value for every $1 invested in R&D).

There was a significant amount of risk associated with this component and the cost of capital was estimated to be 15%.
## Value of Future R&D

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<td>$644.97</td>
<td>$515.98</td>
<td>$128.99</td>
<td>$36.67</td>
</tr>
<tr>
<td>10</td>
<td>$773.97</td>
<td>$619.17</td>
<td>$154.79</td>
<td>$38.26</td>
</tr>
</tbody>
</table>

$318.30
The value of Biogen as a firm is the sum of all three components – the present value of cash flows from existing products, the value of Avonex (as an option) and the value created by new research:

\[
\text{Value} = \text{Existing products} + \text{Existing Patents} + \text{Value: Future R&D} \\
= \$397.13 \text{ million} + \$907 \text{ million} + \$318.30 \text{ million} \\
= \$1,622.43 \text{ million}
\]

Since Biogen had no debt outstanding, this value was divided by the number of shares outstanding (35.50 million) to arrive at a value per share:

\[
\text{Value per share} = \frac{\$1,622.43 \text{ million}}{35.5} = \$45.70
\]
The Real Options Test: Patents and Technology

- **The Option Test:**
  - Underlying Asset: Product that would be generated by the patent
  - Contingency:
    - If PV of CFs from development > Cost of development: PV - Cost
    - If PV of CFs from development < Cost of development: 0

- **The Exclusivity Test:**
  - Patents restrict competitors from developing similar products
  - Patents do not restrict competitors from developing other products to treat the same disease.

- **The Pricing Test**
  - Underlying Asset: Patents are not traded. Not only do you therefore have to estimate the present values and volatilities yourself, you cannot construct replicating positions or do arbitrage.
  - Option: Patents are bought and sold, though not as frequently as oil reserves or mines.
  - Cost of Exercising the Option: This is the cost of converting the patent for commercial production. Here, experience does help and drug firms can make fairly precise estimates of the cost.

- **Conclusion:** You can estimate the value of the real option but the quality of your estimate will be a direct function of the quality of your capital budgeting. It works best if you are valuing a publicly traded firm that generates most of its value from one or a few patents - you can use the market value of the firm and the variance in that value then in your option pricing model.
Example 2: Valuing Natural Resource Options

- In a natural resource investment, the underlying asset is the resource and the value of the asset is based upon two variables - the quantity of the resource that is available in the investment and the price of the resource.

- In most such investments, there is a cost associated with developing the resource, and the difference between the value of the asset extracted and the cost of the development is the profit to the owner of the resource.

- Defining the cost of development as X, and the estimated value of the resource as V, the potential payoffs on a natural resource option can be written as follows:

  Payoff on natural resource investment = \( V - X \) if \( V > X \)
  = 0 if \( V \leq X \)
Payoff Diagram on Natural Resource Firms

Cost of Developing Reserve

Net Payoff on Extraction

Value of estimated reserve of natural resource
## Estimating Inputs for Natural Resource Options

<table>
<thead>
<tr>
<th>Input</th>
<th>Estimation Process</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. Value of Available Reserves of the Resource</td>
<td>• Expert estimates (Geologists for oil..); The present value of the after-tax cash flows from the resource are then estimated.</td>
</tr>
<tr>
<td>2. Cost of Developing Reserve (Strike Price)</td>
<td>• Past costs and the specifics of the investment</td>
</tr>
<tr>
<td>3. Time to Expiration</td>
<td>• Relinquishment Period: if asset has to be relinquished at a point in time. • Time to exhaust inventory - based upon inventory and capacity output.</td>
</tr>
<tr>
<td>4. Variance in value of underlying asset</td>
<td>• based upon variability of the price of the resources and variability of available reserves.</td>
</tr>
<tr>
<td>5. Net Production Revenue (Dividend Yield)</td>
<td>• Net production revenue every year as percent of market value.</td>
</tr>
<tr>
<td>6. Development Lag</td>
<td>• Calculate present value of reserve based upon the lag.</td>
</tr>
</tbody>
</table>
Valuing Gulf Oil

- Gulf Oil was the target of a takeover in early 1984 at $70 per share (it had 165.30 million shares outstanding, and total debt of $9.9 billion).
  - It had estimated reserves of 3038 million barrels of oil and the average cost of developing these reserves was estimated to be $10 a barrel in present value dollars (the development lag is approximately two years).
  - The average relinquishment life of the reserves is 12 years.
  - The price of oil was $22.38 per barrel, and the production cost, taxes and royalties were estimated at $7 per barrel.
  - The bond rate at the time of the analysis was 9.00%.
  - Gulf was expected to have net production revenues each year of approximately 5% of the value of the developed reserves. The variance in oil prices is 0.03.
Valuing Undeveloped Reserves

- **Inputs for valuing undeveloped reserves**
  - Value of underlying asset = Value of estimated reserves discounted back for period of development lag = $22.38 - $7) / 1.05^2 = $42,380.44
  - Exercise price = Estimated development cost of reserves = 3038 * $10 = $30,380 million
  - Time to expiration = Average length of relinquishment option = 12 years
  - Variance in value of asset = Variance in oil prices = 0.03
  - Riskless interest rate = 9%
  - Dividend yield = Net production revenue/ Value of developed reserves = 5%

- **Based upon these inputs, the Black-Scholes model provides the following value for the call:**
  \[
  \begin{align*}
  &d_1 = 1.6548 \quad N(d_1) = 0.9510 \\
  &d_2 = 1.0548 \quad N(d_2) = 0.8542 \\
  \text{Call Value} &= 42,380.44 \exp(-0.05)(12) (0.9510) - 30,380 (\exp(-0.09)(12) (0.8542) \\
  &= $13,306 million
  \end{align*}
  \]
In addition, Gulf Oil had free cashflows to the firm from its oil and gas production of $915 million from already developed reserves and these cashflows are likely to continue for ten years (the remaining lifetime of developed reserves).

The present value of these developed reserves, discounted at the weighted average cost of capital of 12.5%, yields:

- Value of already developed reserves = \(915 \times (1 - 1.125^{-10}) / .125\) = $5065.83

Adding the value of the developed and undeveloped reserves:

- Value of undeveloped reserves = $13,306 million
- Value of production in place = $5,066 million
- Total value of firm = $18,372 million
- Less Outstanding Debt = $9,900 million
- Value of Equity = $8,472 million
- Value per share = $8,472/165.3 = $51.25
B. The Option to Expand/Take Other Projects

- Taking a project today may allow a firm to consider and take other valuable projects in the future.

- Thus, even though a project may have a negative NPV, it may be a project worth taking if the option it provides the firm (to take other projects in the future) provides a more-than-compensating value.

- These are the options that firms often call “strategic options” and use as a rationale for taking on “negative NPV” or even “negative return” projects.
The Option to Expand

PV of Cash Flows from Expansion

Additional Investment to Expand

Firm will not expand in this section

Expansion becomes attractive in this section

Present Value of Expected Cash Flows on Expansion
The option to expand: Valuing a young, start-up company

- You have complete a DCF valuation of a small anti-virus software company, Secure Mail, and estimated a value of $115 million.

- Assume that there is the possibility that the company could use the customer base that it develops for the anti-virus software and the technology on which the software is based to create a database software program sometime in the next 5 years.
  - It will cost Secure Mail about $500 million to develop a new database program, if they decided to do it today.
  - Based upon the information you have now on the potential for a database program, the company can expect to generate about $40 million a year in after-tax cashflows for ten years. The cost of capital for private companies that provide database software is 12%.
  - The annualized standard deviation in firm value at publicly traded database companies is 50%.
  - The five-year treasury bond rate is 3%.
Valuing the Expansion Option

S = Value of entering the database software market
   = PV of $40 million for 10 years @12% = $226 million
K = Exercise price
   = Cost of entering the database software market = $500 million
t = Period over which you have the right to enter the market
   = 5 years
σ = Standard deviation of stock prices of database firms = 50%
r = Riskless rate = 3%

Call Value = $56 Million

DCF valuation of the firm = $115 million
Value of Option to Expand to Database market = $56 million
Value of the company with option to expand = $171 million

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A note of caution: Opportunities are not options...

Is the first investment necessary for the second investment?

Not necessary

Pre-Requisit

A Zero competitive advantage on Second Investment

An Exclusive Right to Second Investment

No option value

Option has no value

Option has high value

Second Investment has zero excess returns

Second investment has large sustainable excess return

First-Mover

Technological Edge

Brand Name

Telecom Licenses

Pharmaceutical patents

Increasing competitive advantage/ barriers to entry

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The Real Options Test for Expansion Options

- **The Options Test**
  - Underlying Asset: Expansion Project
  - Contingency
  - If PV of CF from expansion > Expansion Cost: PV - Expansion Cost
  - If PV of CF from expansion < Expansion Cost: 0

- **The Exclusivity Test**
  - Barriers may range from strong (exclusive licenses granted by the government) to weaker (brand name, knowledge of the market) to weakest (first mover).

- **The Pricing Test**
  - Underlying Asset: As with patents, there is no trading in the underlying asset and you have to estimate value and volatility.
  - Option: Licenses are sometimes bought and sold, but more diffuse expansion options are not.
  - Cost of Exercising the Option: Not known with any precision and may itself evolve over time as the market evolves.

- Using option pricing models to value expansion options will not only yield extremely noisy estimates, but may attach inappropriate premiums to discounted cashflow estimates.
C. The Option to Abandon

- A firm may sometimes have the option to abandon a project, if the cash flows do not measure up to expectations.
- If abandoning the project allows the firm to save itself from further losses, this option can make a project more valuable.

![Diagram showing the relationship between present value of cash flows, cost of abandonment, and decision to abandon a project.](attachment:diagram.png)
Airbus is considering a joint venture with Lear Aircraft to produce a small commercial airplane (capable of carrying 40-50 passengers on short haul flights)
- Airbus will have to invest $500 million for a 50% share of the venture
- Its share of the present value of expected cash flows is 480 million.

Lear Aircraft, which is eager to enter into the deal, offers to buy Airbus’ 50% share of the investment anytime over the next five years for $400 million, if Airbus decides to get out of the venture.

A simulation of the cash flows on this time share investment yields a variance in the present value of the cash flows from being in the partnership is 0.16.

The project has a life of 30 years.
Project with Option to Abandon

- Value of the Underlying Asset (S) = PV of Cash Flows from Project = $480 million
- Strike Price (K) = Salvage Value from Abandonment = $400 million
- Variance in Underlying Asset’s Value = 0.16
- Time to expiration = Life of the Project = 5 years
- Dividend Yield = 1/Life of the Project = 1/30 = 0.033 (We are assuming that the project’s present value will drop by roughly 1/n each year into the project)
- Assume that the five-year riskless rate is 6%. The value of the put option can be estimated.

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Should Airbus enter into the joint venture?

Value of Put = Ke\(^{-rt}\) \(1-N(d2))\) - Se\(^{-yt}\) \(1-N(d1))\)

= 400 exp\((-0.06)(5)\) \((1-0.4624)\) - 480 exp\((-0.033)(5)\) \((1-0.7882)\)

= $73.23 million

□ The value of this abandonment option has to be added on to the net present value of the project of -$20 million, yielding a total net present value with the abandonment option of $53.23 million.
Implications for Investment Analysis/ Valuation

- Having a option to abandon a project can make otherwise unacceptable projects acceptable.

- Other things remaining equal, you would attach more value to companies with
  - More cost flexibility, that is, making more of the costs of the projects into variable costs as opposed to fixed costs.
  - Fewer long-term contracts/obligations with employees and customers, since these add to the cost of abandoning a project.

- These actions will undoubtedly cost the firm some value, but this has to be weighed off against the increase in the value of the abandonment option.
D. Options in Capital Structure

- The most direct applications of option pricing in capital structure decisions is in the design of securities. In fact, most complex financial instruments can be broken down into some combination of a simple bond/common stock and a variety of options.
  - If these securities are to be issued to the public, and traded, the options have to be priced.
  - If these are non-traded instruments (bank loans, for instance), they still have to be priced into the interest rate on the instrument.
- The other application of option pricing is in valuing flexibility. Often, firms preserve debt capacity or hold back on issuing debt because they want to maintain flexibility.
The Value of Flexibility

- Firms maintain excess debt capacity or larger cash balances than are warranted by current needs, to meet unexpected future requirements.

- While maintaining this financing flexibility has value to firms, it also has a cost; the excess debt capacity implies that the firm is giving up some value and has a higher cost of capital.

- The value of flexibility can be analyzed using the option pricing framework; a firm maintains large cash balances and excess debt capacity in order to have the option to take projects that might arise in the future.
The Value of Flexibility

Actual Reinvestment Needs

Expected (Normal) Reinvestment Needs that can be financed without flexibility

Use financing flexibility to take unanticipated investments (acquisitions)

Payoff: \((S-K) \times \text{Excess Return/WACC}\)

Cost of Maintaining Financing Flexibility

Excess Return/WACC = PV of excess returns in perpetuity

Actual Reinvestment Needs
## Disney’s Optimal Debt Ratio

<table>
<thead>
<tr>
<th>Debt Ratio</th>
<th>Cost of Equity</th>
<th>Cost of Debt</th>
<th>Cost of Capital</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.00%</td>
<td>13.00%</td>
<td>4.61%</td>
<td>13.00%</td>
</tr>
<tr>
<td>10.00%</td>
<td>13.43%</td>
<td>4.61%</td>
<td>12.55%</td>
</tr>
<tr>
<td>Current: 18%</td>
<td>13.85%</td>
<td>4.80%</td>
<td>12.22%</td>
</tr>
<tr>
<td>20.00%</td>
<td>13.96%</td>
<td>4.99%</td>
<td>12.17%</td>
</tr>
<tr>
<td>30.00%</td>
<td>14.65%</td>
<td>5.28%</td>
<td>11.84%</td>
</tr>
<tr>
<td>40.00%</td>
<td>15.56%</td>
<td>5.76%</td>
<td>11.64%</td>
</tr>
<tr>
<td>50.00%</td>
<td>16.85%</td>
<td>6.56%</td>
<td>11.70%</td>
</tr>
<tr>
<td>60.00%</td>
<td>18.77%</td>
<td>7.68%</td>
<td>12.11%</td>
</tr>
<tr>
<td>70.00%</td>
<td>21.97%</td>
<td>7.68%</td>
<td>11.97%</td>
</tr>
<tr>
<td>80.00%</td>
<td>28.95%</td>
<td>7.97%</td>
<td>12.17%</td>
</tr>
<tr>
<td>90.00%</td>
<td>52.14%</td>
<td>9.42%</td>
<td>13.69%</td>
</tr>
</tbody>
</table>
# Inputs to Option Valuation Model - Disney

<table>
<thead>
<tr>
<th>Model input</th>
<th>Estimated as</th>
<th>In general…</th>
<th>For Disney</th>
</tr>
</thead>
<tbody>
<tr>
<td>S</td>
<td>Expected annual reinvestment needs (as % of firm value)</td>
<td>Measures magnitude of reinvestment needs</td>
<td>Average of Reinvestment/ Value over last 5 years = 5.3%</td>
</tr>
<tr>
<td>σ²</td>
<td>Variance in annual reinvestment needs</td>
<td>Measures how much volatility there is in investment needs.</td>
<td>Variance over last 5 years in ln(Reinvestment/Value) = 0.375</td>
</tr>
<tr>
<td>K</td>
<td>(Internal + Normal access to external funds)/ Value</td>
<td>Measures the capital constraint</td>
<td>Average over last 5 years = 4.8%</td>
</tr>
<tr>
<td>T</td>
<td>1 year</td>
<td>Measures an annual value for flexibility</td>
<td>T = 1</td>
</tr>
</tbody>
</table>
The value of an option with these characteristics is 1.6092%. You can consider this the value of the option to take a project, but the overall value of flexibility will still depend upon the quality of the projects taken. In other words, the value of the option to take a project is zero if the project has zero net present value.

Disney earns 18.69% on its projects has a cost of capital of 12.22%. The excess return (annually) is 6.47%. Assuming that they can continue to generate these excess returns in perpetuity:
Value of Flexibility (annual) = 1.6092% * (0.0647 / 0.1222) = 0.85% of value

Disney’s cost of capital at its optimal debt ratio is 11.64%. The cost it incurs to maintain flexibility is therefore 0.58% annually (12.22% - 11.64%). It therefore pays to maintain flexibility.
Determinants of the Value of Flexibility

- **Capital Constraints (External and Internal):** The greater the capacity to raise funds, either internally or externally, the less the value of flexibility.
  - 1.1: Firms with significant internal operating cash flows should value flexibility less than firms with small or negative operating cash flows.
  - 1.2: Firms with easy access to financial markets should have a lower value for flexibility than firms without that access.

- **Unpredictability of reinvestment needs:** The more unpredictable the reinvestment needs of a firm, the greater the value of flexibility.

- **Capacity to earn excess returns:** The greater the capacity to earn excess returns, the greater the value of flexibility.
  - 1.3: Firms that do not have the capacity to earn or sustain excess returns get no value from flexibility.
E. Valuing Equity as an option

- The equity in a firm is a residual claim, i.e., equity holders lay claim to all cashflows left over after other financial claim-holders (debt, preferred stock etc.) have been satisfied.

- If a firm is liquidated, the same principle applies, with equity investors receiving whatever is left over in the firm after all outstanding debts and other financial claims are paid off.

- The principle of limited liability, however, protects equity investors in publicly traded firms if the value of the firm is less than the value of the outstanding debt, and they cannot lose more than their investment in the firm.
Payoff Diagram for Liquidation Option

- **Value of firm**
- **Face Value of Debt**
- **Net Payoff on Equity**
Application to valuation: A simple example

- Assume that you have a firm whose assets are currently valued at $100 million and that the standard deviation in this asset value is 40%.
- Further, assume that the face value of debt is $80 million (It is zero coupon debt with 10 years left to maturity).
- If the ten-year treasury bond rate is 10%,
  - how much is the equity worth?
  - What should the interest rate on debt be?

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Model Parameters

- Value of the underlying asset = S
  - Value of the firm = $100 million
- Exercise price = K
  - Face Value of outstanding debt = $80 million
- Life of the option = t
  - Life of zero-coupon debt = 10 years
- Variance in the value of the underlying asset = $\sigma^2$
  - Variance in firm value = 0.16
- Riskless rate = r
  - Treasury bond rate corresponding to option life = 10%
Valuing Equity as a Call Option

- Based upon these inputs, the Black-Scholes model provides the following value for the call:
  \[ d1 = 1.5994 \quad N(d1) = 0.9451 \]
  \[ d2 = 0.3345 \quad N(d2) = 0.6310 \]
- Value of the call = 100 \( 0.9451 \) - 80 \( \exp(-0.10)(10) \) \( 0.6310 \) = $75.94 million
- Value of the outstanding debt = $100 - $75.94 = $24.06 million
- Interest rate on debt = \( ($80 / $24.06)^{1/10} - 1 \) = 12.77%
I. The Effect of Catastrophic Drops in Value

Assume now that a catastrophe wipes out half the value of this firm (the value drops to $50 million), while the face value of the debt remains at $80 million. What will happen to the equity value of this firm?

a. It will drop in value to $25.94 million [$50 million - market value of debt from previous page]

b. It will be worth nothing since debt outstanding > Firm Value

c. It will be worth more than $25.94 million
Valuing Equity in the Troubled Firm

- Value of the underlying asset = \( S \)
  - Value of the firm = $50 million

- Exercise price = \( K \)
  - Face Value of outstanding debt = $80 million

- Life of the option = \( t \)
  - Life of zero-coupon debt = 10 years

- Variance in the value of the underlying asset = \( \sigma^2 \)
  - Variance in firm value = 0.16

- Riskless rate = \( r \)
  - Treasury bond rate corresponding to option life = 10%
The Value of Equity as an Option

Based upon these inputs, the Black-Scholes model provides the following value for the call:

\[ d_1 = 1.0515 \quad N(d_1) = 0.8534 \]
\[ d_2 = -0.2135 \quad N(d_2) = 0.4155 \]

Value of the call = $50 \times 0.8534 - 80 \times \exp\left(-0.10 \times 10\right) \times 0.4155 = \$30.44 \text{ million} \]

Value of the bond = $50 - $30.44 = $19.56 \text{ million} \]

The equity in this firm drops by $45.50 million, less than the overall drop in value of $50 million, because of the option characteristics of equity.

This might explain why stock in firms, which are in Chapter 11 and essentially bankrupt, still has value.
Equity value persists..

Value of Equity as Firm Value Changes

Value of Firm ($ 80 Face Value of Debt)
II. The conflict between stockholders and bondholders

Consider again the firm described in the earlier example, with a value of assets of $100 million, a face value of zero-coupon ten-year debt of $80 million, a standard deviation in the value of the firm of 40%. The equity and debt in this firm were valued as follows:

- Value of Equity = $75.94 million
- Value of Debt = $24.06 million
- Value of Firm = $100 million

Now assume that the stockholders have the opportunity to take a project with a negative net present value of -$2 million, but assume that this project is a very risky project that will push up the standard deviation in firm value to 50%. Would you invest in this project?

a. Yes
b. No
Valuing Equity after the Project

- Value of the underlying asset = S
  - Value of the firm = $100 million - $2 million = $98 million (The value of the firm is lowered because of the negative net present value project)

- Exercise price = K
  - Face Value of outstanding debt = $80 million

- Life of the option = t

- Life of zero-coupon debt = 10 years

- Variance in the value of the underlying asset = $\sigma^2$
  - Variance in firm value = 0.25

- Riskless rate = r
  - Treasury bond rate corresponding to option life = 10%
Option Valuation

- Option Pricing Results for Equity and Debt Value
  - Value of Equity = $77.71
  - Value of Debt = $20.29
  - Value of Firm = $98.00

- The value of equity rises from $75.94 million to $77.71 million, even though the firm value declines by $2 million. The increase in equity value comes at the expense of bondholders, who find their wealth decline from $24.06 million to $20.19 million.
Effects of an Acquisition

Assume that you are the manager of a firm and that you buy another firm, with a fair market value of $150 million, for exactly $150 million. In an efficient market, the stock price of your firm will

a. Increase
b. Decrease
c. Remain Unchanged
You are provided information on two firms, which operate in unrelated businesses and hope to merge.

- **Firm A**
  - Value of the firm: $100 million
  - Face Value of Debt (10 yr zeros): $80 million
  - Maturity of debt: 10 years
  - Std. Dev. in value: 40%
  - Correlation between cashflows: 0.4

- **Firm B**
  - Value of the firm: $150 million
  - Face Value of Debt (10 yr zeros): $50 million
  - Maturity of debt: 10 years
  - Std. Dev. in value: 50%
  - Correlation between cashflows: 0.4

The ten-year bond rate is 10%.

The variance in the value of the firm after the acquisition can be calculated as follows:

\[
\text{Variance in combined firm value} = w_1^2 \sigma_1^2 + w_2^2 \sigma_2^2 + 2 w_1 w_2 \rho_{12} \sigma_1 \sigma_2
\]

\[
= (0.4)^2 (0.16) + (0.6)^2 (0.25) + 2 (0.4) (0.6) (0.4) (0.4) (0.5)
\]

\[
= 0.154
\]
The values of equity and debt in the individual firms and the combined firm can then be estimated using the option pricing model:

<table>
<thead>
<tr>
<th></th>
<th>Firm A</th>
<th>Firm B</th>
<th>Combined firm</th>
</tr>
</thead>
<tbody>
<tr>
<td>Value of equity in the firm</td>
<td>$75.94</td>
<td>$134.47</td>
<td>$207.43</td>
</tr>
<tr>
<td>Value of debt in the firm</td>
<td>$24.06</td>
<td>$15.53</td>
<td>$42.57</td>
</tr>
<tr>
<td>Value of the firm</td>
<td>$100.00</td>
<td>$150.00</td>
<td>$250.00</td>
</tr>
</tbody>
</table>

The combined value of the equity prior to the merger is $210.41 million and it declines to $207.43 million after.

The wealth of the bondholders increases by an equal amount.

There is a transfer of wealth from stockholders to bondholders, as a consequence of the merger. Thus, conglomerate mergers that are not followed by increases in leverage are likely to see this redistribution of wealth occur across claim holders in the firm.
The examples that have been used to illustrate the use of option pricing theory to value equity have made some simplifying assumptions. Among them are the following:

1. There were only two claim holders in the firm - debt and equity.
2. There is only one issue of debt outstanding and it can be retired at face value.
3. The debt has a zero coupon and no special features (convertibility, put clauses etc.)
4. The value of the firm and the variance in that value can be estimated.
# Real World Approaches to Valuing Equity in Troubled Firms: Getting Inputs

<table>
<thead>
<tr>
<th>Input</th>
<th>Estimation Process</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Value of the Firm</strong></td>
<td>• Cumulate market values of equity and debt (or)</td>
</tr>
<tr>
<td></td>
<td>• Value the assets in place using FCFF and WACC (or)</td>
</tr>
<tr>
<td></td>
<td>• Use cumulated market value of assets, if traded.</td>
</tr>
<tr>
<td><strong>Variance in Firm Value</strong></td>
<td>• If stocks and bonds are traded,</td>
</tr>
<tr>
<td></td>
<td>[ \sigma^2_{\text{firm}} = w_e \sigma_e^2 + w_d \sigma_d^2 + 2 w_e w_d \rho_{ed} \sigma_e \sigma_d ]</td>
</tr>
<tr>
<td></td>
<td>where ( \sigma_e^2 ) = variance in the stock price</td>
</tr>
<tr>
<td></td>
<td>( w_e = ) MV weight of Equity</td>
</tr>
<tr>
<td></td>
<td>( \sigma_d^2 ) = the variance in the bond price</td>
</tr>
<tr>
<td></td>
<td>( w_d = ) MV weight of debt</td>
</tr>
<tr>
<td></td>
<td>• If not traded, use variances of similarly rated bonds.</td>
</tr>
<tr>
<td></td>
<td>• Use average firm value variance from the industry in which company operates.</td>
</tr>
<tr>
<td><strong>Value of the Debt</strong></td>
<td>• If the debt is short term, you can use only the face or book value of the debt.</td>
</tr>
<tr>
<td></td>
<td>• If the debt is long term and coupon bearing, add the cumulated nominal value of these coupons to the face value of the debt.</td>
</tr>
<tr>
<td><strong>Maturity of the Debt</strong></td>
<td>• Face value weighted duration of bonds outstanding (or)</td>
</tr>
<tr>
<td></td>
<td>• If not available, use weighted maturity</td>
</tr>
</tbody>
</table>
Valuing Equity as an option - Eurotunnel in early 1998

- Eurotunnel has been a financial disaster since its opening
  - In 1997, Eurotunnel had earnings before interest and taxes of -£56 million and net income of -£685 million
  - At the end of 1997, its book value of equity was -£117 million
- It had £8,865 million in face value of debt outstanding
  - The weighted average duration of this debt was 10.93 years

<table>
<thead>
<tr>
<th>Debt Type</th>
<th>Face Value</th>
<th>Duration</th>
</tr>
</thead>
<tbody>
<tr>
<td>Short term</td>
<td>935</td>
<td>0.50</td>
</tr>
<tr>
<td>10 year</td>
<td>2435</td>
<td>6.7</td>
</tr>
<tr>
<td>20 year</td>
<td>3555</td>
<td>12.6</td>
</tr>
<tr>
<td>Longer</td>
<td>1940</td>
<td>18.2</td>
</tr>
<tr>
<td>Total</td>
<td>£8,865 mil</td>
<td>10.93 years</td>
</tr>
</tbody>
</table>
The Basic DCF Valuation

- The value of the firm estimated using projected cashflows to the firm, discounted at the weighted average cost of capital was £2,312 million.

- This was based upon the following assumptions –
  - Revenues will grow 5% a year in perpetuity.
  - The COGS which is currently 85% of revenues will drop to 65% of revenues in yr 5 and stay at that level.
  - Capital spending and depreciation will grow 5% a year in perpetuity.
  - There are no working capital requirements.
  - The debt ratio, which is currently 95.35%, will drop to 70% after year 5. The cost of debt is 10% in high growth period and 8% after that.
  - The beta for the stock will be 1.10 for the next five years, and drop to 0.8 after the next 5 years.
  - The long term bond rate is 6%.
Other Inputs

- The stock has been traded on the London Exchange, and the annualized std deviation based upon ln (prices) is 41%.
- There are Eurotunnel bonds, that have been traded; the annualized std deviation in ln(price) for the bonds is 17%.
  - The correlation between stock price and bond price changes has been 0.5. The proportion of debt in the capital structure during the period (1992-1996) was 85%.
  - Annualized variance in firm value
    \[= (0.15)^2 (0.41)^2 + (0.85)^2 (0.17)^2 + 2 (0.15) (0.85)(0.5)(0.41)(0.17)\] = 0.0335
- The 15-year bond rate is 6%. (I used a bond with a duration of roughly 11 years to match the life of my option)
Valuing Eurotunnel Equity and Debt

- Inputs to Model
  - Value of the underlying asset = S = Value of the firm = £2,312 million
  - Exercise price = K = Face Value of outstanding debt = £8,865 million
  - Life of the option = t = Weighted average duration of debt = 10.93 years
  - Variance in the value of the underlying asset = \( \sigma^2 \) = Variance in firm value = 0.0335
  - Riskless rate = r = Treasury bond rate corresponding to option life = 6%

- Based upon these inputs, the Black-Scholes model provides the following value for the call:
  - \( d_1 = -0.8337 \) \( N(d_1) = 0.2023 \)
  - \( d_2 = -1.4392 \) \( N(d_2) = 0.0751 \)

- Value of the call = 2312 (0.2023) - 8,865 \( \exp(-0.06)(10.93) \) (0.0751) = £122 million

- Appropriate interest rate on debt = \((8865/2190)^{(1/10.93)}-1\) = 13.65%

Aswath Damodaran
In Closing…

- There are real options everywhere.
- Most of them have no significant economic value because there is no exclusivity associated with using them.
- When options have significant economic value, the inputs needed to value them in a binominal model can be used in more traditional approaches (decision trees) to yield equivalent value.
- The real value from real options lies in
  - Recognizing that building in flexibility and escape hatches into large decisions has value
  - Insights we get on understanding how and why companies behave the way they do in investment analysis and capital structure choices.
Acquirers Anonymous: Seven Steps back to Sobriety...
Great for target companies but not for acquiring company stockholders…

Cumulative Returns: Target and Bidder firms in Public Acquisitions

- The stock price drifts up before the news hits the market.
- The acquisition is announced at this point in time.
- Very slight drift in stock price after announcement.
And the long-term follow up is not positive either.

- Managers often argue that the market is unable to see the long term benefits of mergers that they can see at the time of the deal. If they are right, mergers should create long term benefits to acquiring firms.

- The evidence does not support this hypothesis:
  - McKinsey and Co. has examined acquisition programs at companies on
    - Did the return on capital invested in acquisitions exceed the cost of capital?
    - Did the acquisitions help the parent companies outperform the competition?
    - Half of all programs failed one test, and a quarter failed both.
  - Synergy is elusive. KPMG in a more recent study of global acquisitions concludes that most mergers (>80%) fail - the merged companies do worse than their peer group.
  - A large number of acquisitions that are reversed within fairly short time periods. About 20% of the acquisitions made between 1982 and 1986 were divested by 1988. In studies that have tracked acquisitions for longer time periods (ten years or more) the divestiture rate of acquisitions rises to almost 50%.
The disease is spreading: Indian firms acquiring US targets – 1999 - 2005
Growing through acquisitions seems to be a “loser’s game”

- Firms that grow through acquisitions have generally had far more trouble creating value than firms that grow through internal investments.
- In general, acquiring firms tend to
  - Pay too much for target firms
  - Overestimate the value of “synergy” and “control”
  - Have a difficult time delivering the promised benefits
- Worse still, there seems to be very little learning built into the process. The same mistakes are made over and over again, often by the same firms with the same advisors.
- Conclusion: There is something structurally wrong with the process for acquisitions which is feeding into the mistakes.
The seven sins in acquisitions...

1. Risk Transference: Attributing acquiring company risk characteristics to the target firm.
2. Debt subsidies: Subsiding target firm stockholders for the strengths of the acquiring firm.
3. Auto-pilot Control: The “20% control premium” and other myth...
5. It’s all relative: Transaction multiples, exit multiples...
6. Verdict first, trial afterwards: Price first, valuation to follow
7. It’s not my fault: Holding no one responsible for delivering results.

Aswath Damodaran
## Testing sheet

<table>
<thead>
<tr>
<th>Test</th>
<th>Passed/Failed</th>
<th>Rationalization</th>
</tr>
</thead>
<tbody>
<tr>
<td>Risk transference</td>
<td></td>
<td></td>
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<tr>
<td>Debt subsidies</td>
<td></td>
<td></td>
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<tr>
<td>Control premium</td>
<td></td>
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<tr>
<td>The value of synergy</td>
<td></td>
<td></td>
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<tr>
<td>Comparables and Exit</td>
<td></td>
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</tr>
<tr>
<td>Multiples</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Bias</td>
<td></td>
<td></td>
</tr>
<tr>
<td>A successful acquisition strategy</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Aswath Damodaran
Let's start with a target firm

The target firm has the following income statement:

- Revenues: 100
- Operating Expenses: 80
  \[ \text{Operating Income} = 20 \]
- Taxes: 8
  \[ \text{After-tax OI} = 12 \]

- Assume that this firm will generate this operating income forever (with no growth) and that the cost of equity for this firm is 20%. The firm has no debt outstanding. What is the value of this firm?
Test 1: Risk Transference...

- Assume that as an acquiring firm, you are in a much safer business and have a cost of equity of 10%. What is the value of the target firm to you?
Lesson 1: Don’t transfer your risk characteristics to the target firm

- The cost of equity used for an investment should reflect the risk of the investment and not the risk characteristics of the investor who raised the funds.
- Risky businesses cannot become safe just because the buyer of these businesses is in a safe business.

Aswath Damodaran
Test 2: Cheap debt?

- Assume as an acquirer that you have access to cheap debt (at 4%) and that you plan to fund half the acquisition with debt. How much would you be willing to pay for the target firm?
Lesson 2: Render unto the target firm that which is the target firm’s but not a penny more.

- As an acquiring firm, it is entirely possible that you can borrow much more than the target firm can on its own and at a much lower rate. If you build these characteristics into the valuation of the target firm, you are essentially transferring wealth from your firm’s stockholder to the target firm’s stockholders.

- When valuing a target firm, use a cost of capital that reflects the debt capacity and the cost of debt that would apply to the firm.
Test 3: Control Premiums

- Assume that you are now told that it is conventional to pay a 20% premium for control in acquisitions (backed up by Mergerstat). How much would you be willing to pay for the target firm?

- Would your answer change if I told you that you can run the target firm better and that if you do, you will be able to generate a 30% pre-tax operating margin (rather than the 20% margin that is currently being earned).

- What if the target firm were perfectly run?
Lesson 3: Beware of rules of thumb...

- Valuation is cluttered with rules of thumb. After painstakingly valuing a target firm, using your best estimates, you will be often be told that
  - It is common practice to add arbitrary premiums for brand name, quality of management, control etc...
  - These premiums will be often be backed up by data, studies and services. What they will not reveal is the enormous sampling bias in the studies and the standard errors in the estimates.
  - If you have done your valuation right, those premiums should already be incorporated in your estimated value. Paying a premium will be double counting.
Test 4: Synergy....

- Assume that you are told that the combined firm will be less risky than the two individual firms and that it should have a lower cost of capital (and a higher value). Is this likely?

- Assume now that you are told that there are potential growth and cost savings synergies in the acquisition. Would that increase the value of the target firm?

- Should you pay this as a premium?
The Value of Synergy

Synergy is created when two firms are combined and can be either financial or operating.

Operating Synergy accrues to the combined firm as:

- Strategic Advantages:
  - Higher returns on new investments
    - Higher ROC
    - Higher Growth Rate
  - More new Investments
  - More sustainable excess returns
- Economies of Scale:
  - Cost Savings in current operations
  - Longer Growth Period
- Higher Margin
  - Higher Base-year EBIT

Financial Synergy:
- Tax Benefits:
  - Lower taxes on earnings due to:
    - higher depreciation
    - operating loss carryforwards
- Added Debt Capacity:
  - Higher debt ratio and lower cost of capital
- Diversification?
  - May reduce cost of equity for private or closely held firm
Valuing Synergy

(1) the firms involved in the merger are valued independently, by discounting expected cash flows to each firm at the weighted average cost of capital for that firm.

(2) the value of the combined firm, with no synergy, is obtained by adding the values obtained for each firm in the first step.

(3) The effects of synergy are built into expected growth rates and cashflows, and the combined firm is re-valued with synergy.

Value of Synergy = Value of the combined firm, with synergy - Value of the combined firm, without synergy
**Synergy - Example 1**

**Higher growth and cost savings**

<table>
<thead>
<tr>
<th></th>
<th>P&amp;G</th>
<th>Gillette</th>
<th>Piglet: No Synergy</th>
<th>Piglet: Synergy</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Free Cashflow to Equity</strong></td>
<td>$5,864.74</td>
<td>$1,547.50</td>
<td>$7,412.24</td>
<td>$7,569.73</td>
</tr>
<tr>
<td><strong>Annual operating expenses reduced by $250 million</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Growth rate for first 5 years</strong></td>
<td>12%</td>
<td>10%</td>
<td>11.58%</td>
<td>12.50%</td>
</tr>
<tr>
<td><strong>Slightly higher growth rate</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Growth rate after five years</strong></td>
<td>4%</td>
<td>4%</td>
<td>4.00%</td>
<td>4.00%</td>
</tr>
<tr>
<td><strong>Beta</strong></td>
<td>0.90</td>
<td>0.80</td>
<td>0.88</td>
<td>0.88</td>
</tr>
<tr>
<td><strong>Cost of Equity</strong></td>
<td>7.90%</td>
<td>7.50%</td>
<td>7.81%</td>
<td>7.81%</td>
</tr>
<tr>
<td><strong>Value of synergy</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Value of Equity</strong></td>
<td>$221,292</td>
<td>$59,878</td>
<td>$281,170</td>
<td>$298,355</td>
</tr>
<tr>
<td><strong>Value of synergy</strong></td>
<td></td>
<td></td>
<td></td>
<td>$17,185</td>
</tr>
</tbody>
</table>
Assume that you are Best Buy, the electronics retailer, and that you would like to enter the hardware component of the market. You have been approached by investment bankers for Zenith, which while still a recognized brand name, is on its last legs financially. The firm has net operating losses of $2 billion. If your tax rate is 36%, estimate the tax benefits from this acquisition.

If Best Buy had only $500 million in taxable income, how would you compute the tax benefits?

If the market value of Zenith is $800 million, would you pay this tax benefit as a premium on the market value?
Lesson 4: Don’t pay for buzz words

- Through time, acquirers have always found ways of justifying paying for premiums over estimated value by using buzz words - synergy in the 1980s, strategic considerations in the 1990s and real options in this decade.

- While all of these can have value, the onus should be on those pushing for the acquisitions to show that they do and not on those pushing against them to show that they do not.
Now assume that you are told that an analysis of other acquisitions reveals that acquirers have been willing to pay 5 times EBIT. Given that your target firm has EBIT of $20 million, would you be willing to pay $100 million for the acquisition?

What if I estimate the terminal value using an exit multiple of 5 times EBIT?

As an additional input, your investment banker tells you that the acquisition is accretive. (Your PE ratio is 20 whereas the PE ratio of the target is only 10... Therefore, you will get a jump in earnings per share after the acquisition...)
Biased samples = Poor results

- Biased samples yield biased results. Basing what you pay on what other acquirers have paid is a recipe for disaster. After all, we know that acquirer, on average, pay too much for acquisitions. By matching their prices, we risk replicating their mistakes.

- Even when we use the pricing metrics of other firms in the sector, we may be basing the prices we pay on firms that are not truly comparable.

- When we use exit multiples, we are assuming that what the market is paying for comparable companies today is what it will continue to pay in the future.
Lesson 5: Don’t be a lemming...

- All too often, acquisitions are justified by using one of the following two arguments:
  - Every one else in your sector is doing acquisitions. You have to do the same to survive.
  - The value of a target firm is based upon what others have paid on acquisitions, which may be much higher than what your estimate of value for the firm is.
- With the right set of comparable firms, you can justify almost any price.
- EPS accretion is a meaningless measure. After all, buying an company with a PE lower than yours will lead mathematically to EPS accretion.
Test 6: The CEO really wants to do this... or there are competitive pressures...

- Now assume that you know that the CEO of the acquiring firm really, really wants to do this acquisition and that the investment bankers on both sides have produced fairness opinions that indicate that the firm is worth $100 million. Would you be willing to go along?

- Now assume that you are told that your competitors are all doing acquisitions and that if you don’t do them, you will be at a disadvantage? Would you be willing to go along?
Lesson 6: Don’t let egos or investment bankers get the better of common sense...

- If you define your objective in a bidding war as winning the auction at any cost, you will win. But beware the winner’s curse!

- The premiums paid on acquisitions often have nothing to do with synergy, control or strategic considerations (though they may be provided as the reasons). They may just reflect the egos of the CEOs of the acquiring firms. There is evidence that “over confident” CEOs are more likely to make acquisitions and that they leave a trail across the firms that they run.

- Pre-emptive or defensive acquisitions, where you over pay, either because everyone else is overpaying or because you are afraid that you will be left behind if you don’t acquire are dangerous. If the only way you can stay competitive in a business is by making bad investments, it may be best to think about getting out of the business.
To illustrate: A bad deal is made, and justified by accountants & bankers!

- **HP paid a premium of $5,200 million over the market value.**
- **The difference between the acquisition price ($11,100) and the post-deal book equity ($4,600) was recorded as goodwill ($6,500) on HP's balance sheet.**

**Autonomy: Building up to the acquisition price (in millions)**

- **Pre-deal book equity:** $2,067
- **Post-deal adjusted book equity:** $2,533
- **Pre-deal Market equity:** $4,600
- **Acquisition price:** $11,100
The CEO steps in... and digs a hole...

- Leo Apotheker was the CEO of HP at the time of the deal, brought in to replace Mark Hurd, the previous CEO who was forced to resign because of a “sex” scandal.

- In the face of almost universal feeling that HP had paid too much for Autonomy, Mr. Apotheker addressing a conference at the time of the deal: “We have a pretty rigorous process inside H.P. that we follow for all our acquisitions, which is a D.C.F.-based model,” he said, in a reference to discounted cash flow, a standard valuation methodology. “And we try to take a very conservative view.”

- Apotheker added, “Just to make sure everybody understands, Autonomy will be, on Day 1, accretive to H.P.….. “Just take it from us. We did that analysis at great length, in great detail, and we feel that we paid a very fair price for Autonomy. And it will give a great return to our shareholders.
A year later... HP admits a mistake...and explains it...

- **Premium for non-existent synergy paid by HP ($4,451 m)**
  - Primary culprit: Leo Apotheker (HP's old CEO)
  - Secondary culprits: HP's deal bankers

- **Accounting impropriety effect on synergy ($749 m) and on pre-deal market value ($1,700 m)**
  - Primary culprit: Autonomy's managers
  - Secondary culprit: Deloitte

- **HP's remaining write off ($1,900 m) for post-deal deterioration at Autonomy and/or comparison game playing**
  - Primary culprit: HP's current management
  - Secondary culprits: HP's auditors
Test 7: Is it hopeless?

- The odds seem to be clearly weighted against success in acquisitions. If you were to create a strategy to grow, based upon acquisitions, which of the following offers your best chance of success?

<table>
<thead>
<tr>
<th>This</th>
<th>Or this</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sole Bidder</td>
<td>Bidding War</td>
</tr>
<tr>
<td>Public target</td>
<td>Private target</td>
</tr>
<tr>
<td>Pay with cash</td>
<td>Pay with stock</td>
</tr>
<tr>
<td>Small target</td>
<td>Large target</td>
</tr>
<tr>
<td>Cost synergies</td>
<td>Growth synergies</td>
</tr>
</tbody>
</table>
Better to lose a bidding war than to win one...

Returns in the 40 months before & after bidding war

Source: Malmendier, Moretti & Peters (2011)
Better off buying small rather than large targets... with cash rather than stock
And focusing on private firms and subsidiaries, rather than public firms...
Growth vs Cost Synergies

Top-line trouble: 70 percent of mergers failed to achieve expected revenue synergies

Mergers achieving stated percentage of expected revenue synergies, percent N = 77

<table>
<thead>
<tr>
<th>Percentage Range</th>
<th>Count</th>
</tr>
</thead>
<tbody>
<tr>
<td>&lt;30%</td>
<td>23</td>
</tr>
<tr>
<td>30%-50%</td>
<td>5</td>
</tr>
<tr>
<td>51%-60%</td>
<td>13</td>
</tr>
<tr>
<td>61%-70%</td>
<td>14</td>
</tr>
<tr>
<td>71%-80%</td>
<td>13</td>
</tr>
<tr>
<td>81%-90%</td>
<td>17</td>
</tr>
<tr>
<td>&gt;90%</td>
<td></td>
</tr>
</tbody>
</table>

Typical sources of estimation error

- Ignoring or underestimating customer losses (typically 2% to 5%) that result from the integration
- Assuming growth or share targets out of line with overall market growth and competitive dynamics (no “outside view” calibration)


Cost-synergy estimation is better, but there are patterns emerging in the errors

Mergers achieving stated percentage of expected cost savings, percent N = 92

<table>
<thead>
<tr>
<th>Percentage Range</th>
<th>Count</th>
</tr>
</thead>
<tbody>
<tr>
<td>&lt;30%</td>
<td>3</td>
</tr>
<tr>
<td>30%-50%</td>
<td>5</td>
</tr>
<tr>
<td>51%-60%</td>
<td>1</td>
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<tr>
<td>61%-70%</td>
<td>4</td>
</tr>
<tr>
<td>71%-80%</td>
<td>12</td>
</tr>
<tr>
<td>81%-90%</td>
<td>13</td>
</tr>
<tr>
<td>&gt;90%</td>
<td>25</td>
</tr>
</tbody>
</table>

Typical sources of estimation error

- Underestimating one-time costs
- Using benchmarks from noncomparable situations
- Not sanity-checking management estimates against precedent transactions
- Failing to ground estimates in bottom-up analysis (e.g., location-by-location review of overlaps)

Synergy: Odds of success

- Studies that have focused on synergies have concluded that you are far more likely to deliver cost synergies than growth synergies.
- Synergies that are concrete and planned for at the time of the merger are more likely to be delivered than fuzzy synergies.
- Synergy is much more likely to show up when someone is held responsible for delivering the synergy.
- You are more likely to get a share of the synergy gains in an acquisition when you are a single bidder than if you are one of multiple bidders.
Lesson 7: For acquisitions to create value, you have to stay disciplined.

1. If you have a successful acquisition strategy, stay focused on that strategy. Don’t let size or hubris drive you to “expand” the strategy.

2. Realistic plans for delivering synergy and control have to be put in place before the merger is completed. By realistic, we have to mean that the magnitude of the benefits have to be reachable and not pipe dreams and that the time frame should reflect the reality that it takes a while for two organizations to work as one.

3. The best thing to do in a bidding war is to drop out.

4. Someone (preferably the person pushing hardest for the merger) should be held to account for delivering the benefits.

5. The compensation for investment bankers and others involved in the deal should be tied to how well the deal works rather than for getting the deal done.
VALUE ENHANCEMENT AND THE EXPECTED VALUE OF CONTROL: BACK TO BASICS
The market gives... And takes away....

Figure 1: Cumulative abnormal returns earned around the announcement date by firms changing their names to .com names

New Markets, New Names
In the bull market, adding .com to a company name made a stock soar. Lately those zippy new monikers are disappearing.

New Name, Higher Price
But the stock still get a bounce when dot-com goes away. Chart shows returns in the days before and after the name change.

Sources: Thomson Datastream, P. Raghavendra Ful, Michael J. Cooper, Igor Oselov, Purdue Univ.; Anw Khosana, Virginia Univ.; Ajay Pahl, Wake Forest Univ.
The Paths to Value Creation

- Using the DCF framework, there are four basic ways in which the value of a firm can be enhanced:
  - The cash flows from existing assets to the firm can be increased, by either
    - Increasing after-tax earnings from assets in place or
    - Reducing reinvestment needs (net capital expenditures or working capital)
  - The expected growth rate in these cash flows can be increased by either
    - Increasing the rate of reinvestment in the firm
    - Improving the return on capital on those reinvestments
  - The length of the high growth period can be extended to allow for more years of high growth.
  - The cost of capital can be reduced by
    - Reducing the operating risk in investments/assets
    - Changing the financial mix
    - Changing the financing composition
Value Creation 1: Increase Cash Flows from Assets in Place

More efficient operations and cost cutting: Higher Margins

Divest assets that have negative EBIT

Reduce tax rate
- moving income to lower tax locales
- transfer pricing
- risk management

Revenues
* Operating Margin
= EBIT
- Tax Rate * EBIT
= EBIT (1-t)
+ Depreciation
- Capital Expenditures
- Chg in Working Capital
= FCFF

Live off past over-investment

Better inventory management and tighter credit policies
**Value Creation 2: Increase Value from Expected Growth**

**Pricing Strategies**

*Price Leader versus Volume Leader Strategies*

*Return on Capital = Operating Margin * Capital Turnover Ratio*

- Reinvest more in projects
- Increase operating margins
- Do acquisitions
- Increase capital turnover ratio

**Game theory**

*How will your competitors react to your moves?*

*How will you react to your competitors’ moves?*
Modes of organic growth vary in value creation intensity—consumer goods industry

- **Category of growth**
  - New-product market development
  - Expanding an existing market
  - Maintaining/growing share in a growing market
  - Competing for share in a stable market
  - Acquisition (25th to 75th percentile result)

- **Shareholder value created for incremental $1 million of growth/target acquisition size**
  - New-product market development: 1.75–2.00
  - Expanding an existing market: 0.30–0.75
  - Maintaining/growing share in a growing market: 0.10–0.50
  - Competing for share in a stable market: -0.25–0.40
  - Acquisition (25th to 75th percentile result): -0.5–0.20

- **Revenue growth/acquisition size necessary to double typical company’s share price**
  - New-product market development: 5–6 $ billions
  - Expanding an existing market: 13–33
  - Maintaining/growing share in a growing market: 20–100
  - Competing for share in a stable market: n/m–25
  - Acquisition (25th to 75th percentile result): n/m–50

Aswath Damodaran
Sometimes, growing less is the answer...

Excess Returns: Global Breakdown for 2021

<table>
<thead>
<tr>
<th>Sub Group</th>
<th>Number of firms</th>
<th>&lt;5%</th>
<th>-5% to -2%</th>
<th>-2% to 0%</th>
<th>0 to 2%</th>
<th>2% to 5%</th>
<th>&gt;5%</th>
<th>Positive</th>
<th>Negative</th>
</tr>
</thead>
<tbody>
<tr>
<td>Africa and Middle East</td>
<td>1,913</td>
<td>37.95%</td>
<td>14.69%</td>
<td>14.22%</td>
<td>7.16%</td>
<td>25.08%</td>
<td>39.52%</td>
<td>60.48%</td>
<td></td>
</tr>
<tr>
<td>Australia &amp; NZ</td>
<td>1,510</td>
<td>60.66%</td>
<td>5.23%</td>
<td>7.48%</td>
<td>4.37%</td>
<td>22.25%</td>
<td>30.66%</td>
<td>69.34%</td>
<td></td>
</tr>
<tr>
<td>Canada</td>
<td>2,071</td>
<td>72.34%</td>
<td>4.01%</td>
<td>6.13%</td>
<td>2.95%</td>
<td>14.58%</td>
<td>21.05%</td>
<td>78.95%</td>
<td></td>
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<tr>
<td>China</td>
<td>6,377</td>
<td>27.16%</td>
<td>14.08%</td>
<td>13.88%</td>
<td>8.95%</td>
<td>35.93%</td>
<td>51.73%</td>
<td>48.27%</td>
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</tr>
<tr>
<td>Eastern Europe &amp; Russia</td>
<td>415</td>
<td>30.60%</td>
<td>12.77%</td>
<td>16.14%</td>
<td>9.88%</td>
<td>30.60%</td>
<td>47.95%</td>
<td>52.05%</td>
<td></td>
</tr>
<tr>
<td>EU &amp; Environments</td>
<td>4,698</td>
<td>34.36%</td>
<td>11.56%</td>
<td>12.71%</td>
<td>6.85%</td>
<td>34.53%</td>
<td>47.40%</td>
<td>52.60%</td>
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</tr>
<tr>
<td>India</td>
<td>3,326</td>
<td>33.23%</td>
<td>17.81%</td>
<td>12.62%</td>
<td>7.71%</td>
<td>28.30%</td>
<td>41.37%</td>
<td>58.03%</td>
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</tr>
<tr>
<td>Japan</td>
<td>3,665</td>
<td>17.49%</td>
<td>16.13%</td>
<td>22.05%</td>
<td>10.49%</td>
<td>33.45%</td>
<td>53.70%</td>
<td>46.30%</td>
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<tr>
<td>Latin America &amp; Caribbean</td>
<td>847</td>
<td>31.17%</td>
<td>11.57%</td>
<td>13.70%</td>
<td>8.50%</td>
<td>35.06%</td>
<td>49.23%</td>
<td>50.77%</td>
<td></td>
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<tr>
<td>Small Asia</td>
<td>8,546</td>
<td>35.85%</td>
<td>15.96%</td>
<td>15.37%</td>
<td>8.24%</td>
<td>24.57%</td>
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<td>60.09%</td>
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<tr>
<td>UK</td>
<td>1,037</td>
<td>37.51%</td>
<td>9.35%</td>
<td>10.22%</td>
<td>5.01%</td>
<td>37.90%</td>
<td>48.60%</td>
<td>51.40%</td>
<td></td>
</tr>
<tr>
<td>United States</td>
<td>4,593</td>
<td>39.95%</td>
<td>16.20%</td>
<td>6.88%</td>
<td>5.60%</td>
<td>31.37%</td>
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<td>59.85%</td>
<td></td>
</tr>
<tr>
<td>Global</td>
<td>38,998</td>
<td>35.67%</td>
<td>13.92%</td>
<td>13.17%</td>
<td>7.53%</td>
<td>29.71%</td>
<td>43.40%</td>
<td>56.60%</td>
<td></td>
</tr>
</tbody>
</table>
III. Building Competitive Advantages: Increase length of the growth period

*Increase length of growth period*

- Build on existing competitive advantages
- Find new competitive advantages
  - Brand name
  - Legal Protection
  - Switching Costs
  - Cost advantages
Value Creation 4: Reduce Cost of Capital

Cost of Equity \( \frac{E}{D+E} \) + Pre-tax Cost of Debt \( \frac{D}{D+E} \) = Cost of Capital

- Reduce operating leverage
- Change financing mix
- Make product or service less discretionary to customers
  - Changing product characteristics
  - More effective advertising
- Match debt to assets, reducing default risk
  - Swaps
  - Derivatives
  - Hybrids
SAP: Status Quo

Current Cashflow to Firm

- EBIT(1-t) = 1414
- Net CPX = 831
- Change WC = -19
- FCFF = 602

Reinvestment Rate = 812/1414 = 57.42%

Expected Growth in EBIT (1-t)

0.5742 * 0.1993 = 0.1144

Expected Growth = 11.44%

Stable Growth

- g = 3.41%
- Beta = 1.00
- Debt Ratio = 20%
- Cost of capital = 6.62%
- ROC = 6.62%
- Tax rate = 35%
- Reinvestment Rate = 51.54%

Terminal Value

\[ \text{Terminal Value}_{10} = \frac{1717}{0.0662 - 0.0341} = 53546 \]

Cost of Capital (WACC)

\[ \text{Cost of Capital (WACC)} = 8.77\% \times 0.986 + 2.39\% \times 0.014 = 8.68\% \]

Op. Assets = 31,615

- Cash: 3,018
- Debt: 558
- Pension Lian: 305
- Minor. Int.: 55

Equity = 34,656

Options = 180

Value/Share = 106.12

Cost of Equity = 8.77%

Cost of Debt = (3.41\% + 0.35\%)(1 - 0.3654) = 2.39%

Weights

\[ E = 98.6\% \]

\[ D = 1.4\% \]

Riskfree Rate

Euro riskfree rate = 3.41%

Beta = 1.26

Risk Premium = 4.25%

Unlevered Beta for Sectors = 1.25

Mature risk premium = 4%

Country Equity Prem = 0.25%

Aswath Damodaran

Return on Capital = 19.93%

On May 5, 2005, SAP was trading at 122 Euros/share
<table>
<thead>
<tr>
<th>Debt Ratio</th>
<th>Beta</th>
<th>Cost of Equity</th>
<th>Bond Rating</th>
<th>Interest rate on debt</th>
<th>Tax Rate</th>
<th>Cost of Debt (after-tax)</th>
<th>WACC</th>
<th>Firm Value (G)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0%</td>
<td>1.25</td>
<td>8.72%</td>
<td>AAA</td>
<td>3.76%</td>
<td>36.54%</td>
<td>2.39%</td>
<td>8.72%</td>
<td>$39,088</td>
</tr>
<tr>
<td>10%</td>
<td>1.34</td>
<td>9.09%</td>
<td>AAA</td>
<td>3.76%</td>
<td>36.54%</td>
<td>2.39%</td>
<td>8.42%</td>
<td>$41,480</td>
</tr>
<tr>
<td>20%</td>
<td>1.45</td>
<td>9.56%</td>
<td>A</td>
<td>4.26%</td>
<td>36.54%</td>
<td>2.70%</td>
<td>8.19%</td>
<td>$43,567</td>
</tr>
<tr>
<td>30%</td>
<td>1.59</td>
<td>10.16%</td>
<td>A-</td>
<td>4.41%</td>
<td>36.54%</td>
<td>2.80%</td>
<td>7.95%</td>
<td>$45,900</td>
</tr>
<tr>
<td>40%</td>
<td>1.78</td>
<td>10.96%</td>
<td>CCC</td>
<td>11.41%</td>
<td>36.54%</td>
<td>7.24%</td>
<td>9.47%</td>
<td>$34,043</td>
</tr>
<tr>
<td>50%</td>
<td>2.22</td>
<td>12.85%</td>
<td>C</td>
<td>15.41%</td>
<td>22.08%</td>
<td>12.01%</td>
<td>12.43%</td>
<td>$22,444</td>
</tr>
<tr>
<td>60%</td>
<td>2.78</td>
<td>15.21%</td>
<td>C</td>
<td>15.41%</td>
<td>18.40%</td>
<td>12.58%</td>
<td>13.63%</td>
<td>$19,650</td>
</tr>
<tr>
<td>70%</td>
<td>3.70</td>
<td>19.15%</td>
<td>C</td>
<td>15.41%</td>
<td>15.77%</td>
<td>12.98%</td>
<td>14.83%</td>
<td>$17,444</td>
</tr>
<tr>
<td>80%</td>
<td>5.55</td>
<td>27.01%</td>
<td>C</td>
<td>15.41%</td>
<td>13.80%</td>
<td>13.28%</td>
<td>16.03%</td>
<td>$15,658</td>
</tr>
<tr>
<td>90%</td>
<td>11.11</td>
<td>50.62%</td>
<td>C</td>
<td>15.41%</td>
<td>12.26%</td>
<td>13.52%</td>
<td>17.23%</td>
<td>$14,181</td>
</tr>
</tbody>
</table>
SAP: Restructured

Current Cashflow to Firm

EBIT(1-t) : 1414
- Nt CpX 831
- Chg WC -19
= FCFF 602
Reinvestment Rate = 812/1414
=57.42%

Expected Growth in EBIT (1-t)
.70*.1993=.1144
13.99%

Expected Growth
in EBIT (1-t)
.70*.1993=.1144
13.99%

Reinvestment Rate = 70%

Return on Capital
19.93%

Stable Growth
\( g = 3.41\%; \ \beta = 1.00; \ \) Debit Ratio 30%
Cost of capital = 6.27%
ROI = 6.27\%; Tax rate 35%
Reinvestment Rate = 54.38%

Terminal Value
\[ 10 = \frac{1898}{0.0627 - 0.0341} = 66367 \]

First 5 years

<table>
<thead>
<tr>
<th>Year</th>
<th>EBIT</th>
<th>EBIT(1-t)</th>
<th>Reinvest</th>
<th>FCFF</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>2,543</td>
<td>1,614</td>
<td>1,130</td>
<td>484</td>
</tr>
<tr>
<td>2</td>
<td>2,898</td>
<td>1,839</td>
<td>1,288</td>
<td>552</td>
</tr>
<tr>
<td>3</td>
<td>3,304</td>
<td>2,097</td>
<td>1,468</td>
<td>629</td>
</tr>
<tr>
<td>4</td>
<td>3,766</td>
<td>2,390</td>
<td>1,673</td>
<td>717</td>
</tr>
<tr>
<td>5</td>
<td>4,293</td>
<td>2,724</td>
<td>1,907</td>
<td>817</td>
</tr>
<tr>
<td>6</td>
<td>4,802</td>
<td>3,047</td>
<td>2,011</td>
<td>1,036</td>
</tr>
<tr>
<td>7</td>
<td>5,271</td>
<td>3,345</td>
<td>2,074</td>
<td>1,271</td>
</tr>
<tr>
<td>8</td>
<td>5,673</td>
<td>3,600</td>
<td>2,089</td>
<td>1,512</td>
</tr>
<tr>
<td>9</td>
<td>5,987</td>
<td>3,799</td>
<td>2,052</td>
<td>1,747</td>
</tr>
<tr>
<td>10</td>
<td>6,191</td>
<td>3,929</td>
<td>1,965</td>
<td>1,963</td>
</tr>
</tbody>
</table>

Year 11

EBIT 11,841
EBIT(1-t) 8,433
Reinvest 6,457
FCFF 2,876

Cost of Capital (WACC) = 10.57\% (0.70) + 2.80\% (0.30) = 8.24\%

Cost of Equity 10.57\%

Cost of Debt
\( (3.41\% + 1.00\%) (1 - 0.3654) = 2.80\% \)

Weights
\( E = 70\%\) \( D = 30\% \)

Riskfree Rate:
Euro riskfree rate = 3.41\%

Risk Premium
4.50\%

Mature risk premium
4\%

Country Equity Prem
0.5\%

On May 5, 2005, SAP was trading at 122 Euros/share

Use more debt financing.
Blockbuster: Status Quo

Current Cashflow to Firm

EBIT(1-t) : 163
- Nt CpX : 39
- Chg WC : 4
= FCFF : 120
Reinvestment Rate = 43/163 = 26.46%

Expected Growth in EBIT (1-t)

.2645*.0406=.0107 1.07%

Expected Growth in EBIT (1-t)

1.07%

Expected Growth in EBIT (1-t)

Stable Growth

g = 3%; Beta = 1.00;
Cost of capital = 6.76%
ROC = 6.76%; Tax rate = 35%
Reinvestment Rate = 44.37%

Terminal Value

5
104/(0.0676-.03) = 2714

Discount at Cost of Capital (WACC) = 8.50% (.486) + 3.97% (0.514) = 6.17%

Cost of Equity

8.50%

Cost of Debt

(4.10%+2%)(1-.35) = 3.97%

Weights

E = 48.6% D = 51.4%

Riskfree Rate:

Riskfree rate = 4.10%

Beta

1.10

Risk Premium

4%

Unlevered Beta for Sectors: 0.80

Firm's D/E Ratio: 21.35%

Mature risk premium 4%

Country Equity Prem 0%

Value/Share $ 5.13

Op. Assets 2,472
+ Cash: 330
- Debt 1847
= Equity 955
- Options 0

Term Yr

184
82
102

Return on Capital 4.06%
Current Cashflow to Firm

EBIT(1-t) : 249
- Nt CpX : 39
- Chg WC : 4
= FCFF : 206
Reinvestment Rate = 43/249
= 17.32%

Expected Growth in EBIT (1-t)
.1732*.0620 = .0107
1.07%

Stable Growth
g = 3%; Beta = 1.00;
Cost of capital = 6.76%
ROC = 6.76%; Tax rate = 35%
Reinvestment Rate = 44.37%

Expected Growth
in EBIT (1-t)
.1732*.0620 = .0107
1.07%

+ Cash : 330
- Debt : 1847
= Equity : 2323
- Options : 0
Value/Share $ 12.47

EBIT (1-t)
1 2 3 4 5
$252 $255 $258 $264 $272
- Reinvestment
$ 44 $ 44 $ 59 $ 89 $121
FCFF
$208 $211 $200 $176 $151

Discount at Cost of Capital (WACC) = 8.50% (.486) + 3.97% (0.514) = 6.17%

Cost of Equity
8.50%

Cost of Debt
(4.10%+2%)(1-.35) = 3.97%

Weights
E = 48.6% D = 51.4%

Riskfree Rate:
Riskfree rate = 4.10%

Risk premium
4%

Beta
1.10

Unlevered Beta for Sectors: 0.80
Firm's D/E Ratio: 21.35%
Mature risk premium 4%
Country Equity Prem 0%
The Expected Value of Control

The Value of Control

Probability that you can change the management of the firm \times \text{Change in firm value from changing management}

- Takeover Restrictions
- Voting Rules & Rights
- Access to Funds
- Size of company

Value of the firm run optimally

- Value of the firm run status quo
Why the probability of management changing shifts over time....

- Corporate governance rules can change over time, as new laws are passed. If the change gives stockholders more power, the likelihood of management changing will increase.

- Activist investing ebbs and flows with market movements (activist investors are more visible in down markets) and often in response to scandals.

- Events such as hostile acquisitions can make investors reassess the likelihood of change by reminding them of the power that they do possess.
Estimating the Probability of Change

You can estimate the probability of management changes by using historical data (on companies where change has occurred) and statistical techniques such as probits or logits.

Empirically, the following seem to be related to the probability of management change:

- Stock price and earnings performance, with forced turnover more likely in firms that have performed poorly relative to their peer group and to expectations.

- Structure of the board, with forced CEO changes more likely to occur when the board is small, is composed of outsiders and when the CEO is not also the chairman of the board of directors.

- Ownership structure, since forced CEO changes are more common in companies with high institutional and low insider holdings. They also seem to occur more frequently in firms that are more dependent upon equity markets for new capital.

- Industry structure, with CEOs more likely to be replaced in competitive industries.
Manifestations of the Value of Control

- Hostile acquisitions: In hostile acquisitions which are motivated by control, the control premium should reflect the change in value that will come from changing management.

- Valuing publicly traded firms: The market price for every publicly traded firm should incorporate an expected value of control, as a function of the value of control and the probability of control changing.
  
  \[
  \text{Market value} = \text{Status quo value} + (\text{Optimal value} - \text{Status quo value}) \times \text{Probability of management changing}
  \]

- Voting and non-voting shares: The premium (if any) that you would pay for a voting share should increase with the expected value of control.

- Minority Discounts in private companies: The minority discount (attached to buying less than a controlling stake) in a private business should be increase with the expected value of control.
1. Hostile Acquisition: Example

- In a hostile acquisition, you can ensure management change after you take over the firm. Consequently, you would be willing to pay up to the optimal value.

- As an example, Blockbuster was trading at $9.50 per share in July 2005. The optimal value per share that we estimated as $12.47 per share. Assuming that this is a reasonable estimate, you would be willing to pay up to $2.97 as a premium in acquiring the shares.

- Issues to ponder:
  - Would you automatically pay $2.97 as a premium per share? Why or why not?
  - What would your premium per share be if change will take three years to implement?
2. Market prices of Publicly Traded Companies: An example

- The market price per share at the time of the valuation (May 2005) was roughly $9.50.
  - Expected value per share = Status Quo Value + Probability of control changing * (Optimal Value – Status Quo Value)
  - $9.50 = $5.13 + Probability of control changing ($12.47 - $5.13)

- The market is attaching a probability of 59.5% that management policies can be changed. This was after Icahn’s successful challenge of management. Prior to his arriving, the market price per share was $8.20, yielding a probability of only 41.8% of management changing.

<table>
<thead>
<tr>
<th></th>
<th>Value of Equity</th>
<th>Value per share</th>
</tr>
</thead>
<tbody>
<tr>
<td>Status Quo</td>
<td>$955 million</td>
<td>$5.13 per share</td>
</tr>
<tr>
<td>Optimally managed</td>
<td>$2,323 million</td>
<td>$12.47 per share</td>
</tr>
</tbody>
</table>
Value of stock in a publicly traded firm

When a firm is badly managed, the market still assesses the probability that it will be run better in the future and attaches a value of control to the stock price today:

$$\text{Value per share} = \frac{\text{Status Quo Value} + \text{Probability of control change (Optimal - Status Quo Value)}}{\text{Number of shares outstanding}}$$

With voting shares and non-voting shares, a disproportionate share of the value of control will go to the voting shares. In the extreme scenario where non-voting shares are completely unprotected:

$$\text{Value per non-voting share} = \frac{\text{Status Quo Value}}{\# \text{ Voting Shares} + \# \text{ Non-voting shares}}$$

$$\text{Value per voting share} = \text{Value of non-voting share} + \frac{\text{Probability of control change (Optimal - Status Quo Value)}}{\# \text{ Voting Shares}}$$
3. Voting and Non-voting Shares: An Example

- To value voting and non-voting shares, we will consider Embraer, the Brazilian aerospace company. As is typical of most Brazilian companies, the company has common (voting) shares and preferred (non-voting shares).
  - Status Quo Value = 12.5 billion $R for the equity;
  - Optimal Value = 14.7 billion $R, assuming that the firm would be more aggressive both in its use of debt and in its reinvestment policy.

- There are 242.5 million voting shares and 476.7 non-voting shares in the company and the probability of management change is relatively low. Assuming a probability of 20% that management will change, we estimated the value per non-voting and voting share:
  - Value per non-voting share = Status Quo Value/ (# voting shares + # non-voting shares) = 12,500/(242.5+476.7) = 17.38 $R/ share
  - Value per voting share = Status Quo value/sh + Probability of management change * (Optimal value – Status Quo Value) = 17.38 + 0.2* (14,700-12,500)/242.5 = 19.19 $R/share

- With our assumptions, the voting shares should trade at a premium of 10.4% over the non-voting shares.
Assume that you are valuing Kristin Kandy, a privately owned candy business for sale in a private transaction. You have estimated a value of $1.6 million for the equity in this firm, assuming that the existing management of the firm continues into the future and a value of $2 million for the equity with new and more creative management in place.

- Value of 51% of the firm = 51% of optimal value = 0.51 * $2 million = $1.02 million
- Value of 49% of the firm = 49% of status quo value = 0.49 * $1.6 million = $784,000

Note that a 2% difference in ownership translates into a large difference in value because one stake ensures control and the other does not.
Alternative Approaches to Value Enhancement

Maximize a variable that is correlated with the value of the firm. There are several choices for such a variable. It could be:
- an accounting variable, such as earnings or return on investment
- a marketing variable, such as market share
- a cash flow variable, such as cash flow return on investment (CFROI)
- a risk-adjusted cash flow variable, such as Economic Value Added (EVA)

The advantages of using these variables are that they:
- Are often simpler and easier to use than DCF value.

The disadvantage is that the:
- Simplicity comes at a cost; these variables are not perfectly correlated with DCF value.
The Economic Value Added (EVA) is a measure of surplus value created on an investment.

- Define the return on capital (ROC) to be the “true” cash flow return on capital earned on an investment.
- Define the cost of capital as the weighted average of the costs of the different financing instruments used to finance the investment.
- EVA = (Return on Capital - Cost of Capital) (Capital Invested in Project)

The CFROI is a measure of the cash flow return made on capital

- It is computed as an IRR, based upon a base value of capital invested and the cash flow on that capital.
The bottom line...

- The value of a firm is not going to change just because you use a different metric for value. All approaches that are discounted cash flow approaches should yield the same value for a business, if they make consistent assumptions.

- If there are differences in value from using different approaches, they must be attributable to differences in assumptions, either explicit or implicit, behind the valuation.
A Simple Illustration

- Assume that you have a firm with a book value value of capital of $100 million, on which it expects to generate a return on capital of 15% in perpetuity with a cost of capital of 10%.

- This firm is expected to make additional investments of $10 million at the beginning of each year for the next 5 years. These investments are also expected to generate 15% as return on capital in perpetuity, with a cost of capital of 10%.

- After year 5, assume that
  - The earnings will grow 5% a year in perpetuity.
  - The firm will keep reinvesting back into the business but the return on capital on these new investments will be equal to the cost of capital (10%).
Firm Value using EVA Approach

Capital Invested in Assets in Place = $100

EVA from Assets in Place = (.15 - .10) * (100)/.10 = $50

+ PV of EVA from New Investments in Year 1 = [(1.15 - .10)(10)/.10] = $5

+ PV of EVA from New Investments in Year 2 = [(1.15 - .10)(10)/.10]/1.1 = $4.55

+ PV of EVA from New Investments in Year 3 = [(1.15 - .10)(10)/.10]/1.1^2 = $4.13

+ PV of EVA from New Investments in Year 4 = [(1.15 - .10)(10)/.10]/1.1^3 = $3.76

+ PV of EVA from New Investments in Year 5 = [(1.15 - .10)(10)/.10]/1.1^4 = $3.42

Value of Firm = $170.85
### Firm Value using DCF Valuation: Estimating FCFF

<table>
<thead>
<tr>
<th></th>
<th>Base Year</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>Term. Year</th>
</tr>
</thead>
<tbody>
<tr>
<td>EBIT (1-t) : Assets in Place</td>
<td>$15.00</td>
<td>$15.00</td>
<td>$15.00</td>
<td>$15.00</td>
<td>$15.00</td>
<td>$15.00</td>
<td></td>
</tr>
<tr>
<td>EBIT(1-t) :Investments- Yr 1</td>
<td>$1.50</td>
<td>$1.50</td>
<td>$1.50</td>
<td>$1.50</td>
<td>$1.50</td>
<td>$1.50</td>
<td></td>
</tr>
<tr>
<td>EBIT(1-t) :Investments- Yr 2</td>
<td>$1.50</td>
<td>$1.50</td>
<td>$1.50</td>
<td>$1.50</td>
<td>$1.50</td>
<td>$1.50</td>
<td></td>
</tr>
<tr>
<td>EBIT(1-t): Investments -Yr 3</td>
<td>$1.50</td>
<td>$1.50</td>
<td>$1.50</td>
<td>$1.50</td>
<td>$1.50</td>
<td></td>
<td></td>
</tr>
<tr>
<td>EBIT(1-t): Investments -Yr 4</td>
<td></td>
<td>$1.50</td>
<td>$1.50</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>EBIT(1-t): Investments- Yr 5</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>$1.50</td>
<td></td>
</tr>
<tr>
<td>Total EBIT(1-t)</td>
<td>$16.50</td>
<td>$18.00</td>
<td>$19.50</td>
<td>$21.00</td>
<td>$22.50</td>
<td>$23.63</td>
<td></td>
</tr>
<tr>
<td>- Net Capital Expenditures</td>
<td>$10.00</td>
<td>$10.00</td>
<td>$10.00</td>
<td>$10.00</td>
<td>$10.00</td>
<td>$11.25</td>
<td></td>
</tr>
<tr>
<td>FCFF</td>
<td>$6.50</td>
<td>$8.00</td>
<td>$9.50</td>
<td>$11.00</td>
<td>$11.25</td>
<td>$11.81</td>
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</tr>
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</table>

After year 5, the reinvestment rate is 50% = g/ ROC
### Firm Value: Present Value of FCFF

<table>
<thead>
<tr>
<th>Year</th>
<th>0</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>Term Year</th>
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</thead>
<tbody>
<tr>
<td><strong>FCFF</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>$6.50</td>
<td>$8.00</td>
<td>$9.50</td>
<td>$11.00</td>
<td>$11.25</td>
<td>$11.81</td>
<td></td>
</tr>
<tr>
<td><strong>PV of FCFF</strong></td>
<td>($10)</td>
<td>$5.91</td>
<td>$6.61</td>
<td>$7.14</td>
<td>$7.51</td>
<td>$6.99</td>
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</tr>
<tr>
<td><strong>Terminal Value</strong></td>
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<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>$236.25</td>
</tr>
<tr>
<td><strong>PV of Terminal Value</strong></td>
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<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>$146.69</td>
</tr>
<tr>
<td><strong>Value of Firm</strong></td>
<td><strong>$170.85</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Implications

- Growth, by itself, does not create value. It is growth, with investment in excess return projects, that creates value.
  - The growth of 5% a year after year 5 creates no additional value.
- The “market value added” (MVA), which is defined to be the excess of market value over capital invested is a function of the excess value created.
  - In the example above, the market value of $170.85 million exceeds the book value of $100 million, because the return on capital is 5% higher than the cost of capital.
Year-by-year EVA Changes

- Firms are often evaluated based upon year-to-year changes in EVA rather than the present value of EVA over time.
- The advantage of this comparison is that it is simple and does not require the making of forecasts about future earnings potential.
- Another advantage is that it can be broken down by any unit - person, division etc., as long as one is willing to assign capital and allocate earnings across these same units.
- While it is simpler than DCF valuation, using year-by-year EVA changes comes at a cost. In particular, it is entirely possible that a firm which focuses on increasing EVA on a year-to-year basis may end up being less valuable.
Gaming the system: Delivering high current EVA while destroying value...

- **The Growth trade off game:** Managers may give up valuable growth opportunities in the future to deliver higher EVA in the current year.

- **The Risk game:** Managers may be able to deliver a higher dollar EVA but in riskier businesses. The value of the business is the present value of EVA over time and the risk effect may dominate the increased EVA.

- **The Capital Invested game:** The key to delivering positive EVA is to make investments that do not show up as part of capital invested. That way, your operating income will increase while capital invested will decrease.
Delivering a high EVA may not translate into higher stock prices...

- The relationship between EVA and Market Value Changes is more complicated than the one between EVA and Firm Value.
- The market value of a firm reflects not only the Expected EVA of Assets in Place but also the Expected EVA from Future Projects.
- To the extent that the actual economic value added is smaller than the expected EVA the market value can decrease even though the EVA is higher.

Aswath Damodaran
When focusing on year-to-year EVA changes has least side effects

1. Most or all of the assets of the firm are already in place; i.e., very little or none of the value of the firm is expected to come from future growth.
   - This minimizes the risk that increases in current EVA come at the expense of future EVA

2. The leverage is stable and the cost of capital cannot be altered easily by the investment decisions made by the firm.
   - This minimizes the risk that the higher EVA is accompanied by an increase in the cost of capital

3. The firm is in a sector where investors anticipate little or not surplus returns; i.e., firms in this sector are expected to earn their cost of capital.
   - This minimizes the risk that the increase in EVA is less than what the market expected it to be, leading to a drop in the market price.